

# Package ‘distrEx’

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**Title** Extensions of Package 'distr'

**Description** Extends package 'distr' by functionals, distances, and conditional distributions.

**Depends** R(>= 3.4), methods, distr(>= 2.8.0)

**Imports** startupmsg(>= 1.0.0), utils, stats

**Suggests** tcltk

**Enhances** robustbase

**ByteCompile** yes

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**Author** Matthias Kohl [cre, cph],  
Peter Ruckdeschel [aut, cph]

**Maintainer** Matthias Kohl <Matthias.Kohl@stamats.de>

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## Contents

distrEx-package . . . . .	2
AbscontCondDistribution-class . . . . .	6
AsymTotalVarDist . . . . .	7
Condition-class . . . . .	11

ContaminationSize . . . . .	12
ConvexContamination . . . . .	13
CvMDist . . . . .	14
dim-methods . . . . .	16
DiscreteCondDistribution-class . . . . .	16
DiscreteMVDistribution . . . . .	18
DiscreteMVDistribution-class . . . . .	19
distrExIntegrate . . . . .	20
distrExMASK . . . . .	23
distrExMOVED . . . . .	23
distrExOptions . . . . .	24
E . . . . .	26
EmpiricalMVDistribution . . . . .	36
EuclCondition . . . . .	37
EuclCondition-class . . . . .	38
GLIntegrate . . . . .	39
HellingerDist . . . . .	40
KolmogorovDist . . . . .	43
liesInSupport . . . . .	45
LMCondDistribution . . . . .	46
LMPParameter . . . . .	47
LMPParameter-class . . . . .	48
m1df . . . . .	49
m2df . . . . .	50
make01 . . . . .	52
MultivariateDistribution-class . . . . .	53
OAsymTotalVarDist . . . . .	54
plot-methods . . . . .	57
PrognCondDistribution . . . . .	58
PrognCondDistribution-class . . . . .	59
PrognCondition-class . . . . .	60
TotalVarDist . . . . .	61
UnivariateCondDistribution-class . . . . .	64
var . . . . .	65

**Index****76**


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**distrEx-package**      *distrEx – Extensions of Package distr*

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**Description**

**distrEx** provides some extensions of package **distr**:

- expectations in the form
  - $E(X)$  for the expectation of a distribution object  $X$
  - $E(X, f)$  for the expectation of  $f(X)$  where  $X$  is some distribution object and  $f$  some function in  $X$

- further functionals: var, sd, IQR, mad, median, skewness, kurtosis
- truncated moments,
- distances between distributions (Hellinger, Cramer von Mises, Kolmogorov, total variation, "convex contamination")
- lists of distributions,
- conditional distributions in factorized form
- conditional expectations in factorized form

Support for extreme value distributions has moved to package **RobExtremes**

## Details

Package:	distrEx
Version:	2.9.6
Date:	2025-01-11
Depends:	R(>= 3.4), methods, distr(>= 2.8.0)
Imports:	startupmsg(>= 1.0.0), utils, stats
Suggests:	tcltk
LazyLoad:	yes
License:	LGPL-3
URL:	<a href="https://distr.r-forge.r-project.org/">https://distr.r-forge.r-project.org/</a>
VCS/SVNRevision:	1482

## Classes

```

Distribution Classes
"Distribution" (from distr)
|>"UnivariateDistribution" (from distr)
|>|"AbscontDistribution" (from distr)
|>|>"Gumbel" (moved to package 'RobExtremes')
|>|>"Pareto" (moved to package 'RobExtremes')
|>|>"GPareto" (moved to package 'RobExtremes')
|>"MultivariateDistribution"
|>|"DiscreteMVDistribution-class"
|>"UnivariateCondDistribution"
|>|"AbscontCondDistribution"
|>|>"PrognCondDistribution"
|>|"DiscreteCondDistribution"
Condition Classes
"Condition"
|>"EuclCondition"
|>"PrognCondition"
Parameter Classes
"OptionalParameter" (from distr)

```

```
|>"Parameter" (from distr)
|>|"LMPParameter"
|>|"GumbelParameter"
|>|"ParetoParameter"
```

## Functions

Integration:	
GLIntegrate	Gauss-Legendre quadrature
distrExIntegrate	Integration of one-dimensional functions
Options:	
distrExOptions	Function to change the global variables of the package 'distrEx'
Standardization:	
make01	Centering and standardization of univariate distributions

## Generating Functions

Distribution Classes	
ConvexContamination	Generic function for generating convex contaminations
DiscreteMVDistribution	Generating function for DiscreteMVDistribution-class
Gumbel	Generating function for Gumbel-class
LMCondDistribution	Generating function for the conditional distribution of a linear regression model.
Condition Classes	
EuclCondition	Generating function for EuclCondition-class
Parameter Classes	
LMPParameter	Generating function for LMPParameter-class

## Methods

Distances:	
ContaminationSize	Generic function for the computation of the convex contamination (Pseudo-)distance of two distributions
HellingerDist	Generic function for the computation of the Hellinger distance of two distributions
KolmogorovDist	Generic function for the computation of the Kolmogorov distance of two distributions
TotalVarDist	Generic function for the computation of the total variation distance of two distributions
AsymTotalVarDist	Generic function for the computation of the asymmetric total variation distance of two distributions (for given ratio rho of negative to positive part of deviation)
OAsymTotalVarDist	Generic function for the computation of the minimal (in rho)

	asymmetric total variation distance of two distributions
vonMisesDist	Generic function for the computation of the von Mises distance of two distributions
liesInSupport	Generic function for testing the support of a distribution
Functionals:	
E	Generic function for the computation of (conditional) expectations
var	Generic functions for the computation of functionals
IQR	Generic functions for the computation of functionals
sd	Generic functions for the computation of functionals
mad	Generic functions for the computation of functionals
median	Generic functions for the computation of functionals
skewness	Generic functions for the computation of functionals
kurtosis	Generic functions for the computation of Functionals
truncated Moments:	
m1df	Generic function for the computation of clipped first moments
m2df	Generic function for the computation of clipped second moments

## Demos

Demos are available — see `demo(package="distrEx")`.

## Acknowledgement

G. Jay Kerns, <gkerns@ysu.edu>, has provided a major contribution, in particular the functionals skewness and kurtosis are due to him.

## Start-up-Banner

You may suppress the start-up banner/message completely by setting `options("StartupBanner"="off")` somewhere before loading this package by `library` or `require` in your R-code / R-session. If option `"StartupBanner"` is not defined (default) or setting `options("StartupBanner"=NULL)` or `options("StartupBanner"="complete")` the complete start-up banner is displayed. For any other value of option `"StartupBanner"` (i.e., not in `c(NULL, "off", "complete")`) only the version information is displayed. The same can be achieved by wrapping the `library` or `require` call into either `suppressStartupMessages()` or `onlytypeStartupMessages(., atypes="version")`.

As for general `packageStartupMessage`'s, you may also suppress all the start-up banner by wrapping the `library` or `require` call into `suppressPackageStartupMessages()` from **startupmsg**-version 0.5 on.

## Package versions

Note: The first two numbers of package versions do not necessarily reflect package-individual development, but rather are chosen for the distrXXX family as a whole in order to ease updating "depends" information.

## Note

Some functions of package **stats** have intentionally been masked, but completely retain their functionality — see `distrExMASK()`. If any of the packages **e1071**, **moments**, **fBasics** is to be used together with **distrEx** the latter must be attached *after* any of the first mentioned. Otherwise `kurtosis()` and `skewness()` defined as *methods* in **distrEx** may get masked.  
To re-mask, you may use `kurtosis <- distrEx::kurtosis`; `skewness <- distrEx::skewness`. See also `distrExMASK()`

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de> and  
 Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>,  
*Maintainer:* Matthias Kohl <Matthias.Kohl@stamats.de>

## References

P. Ruckdeschel, M. Kohl, T. Stabla, F. Camphausen (2006): S4 Classes for Distributions, *R News*, 6(2), 2-6. [https://CRAN.R-project.org/doc/Rnews/Rnews\\_2006-2.pdf](https://CRAN.R-project.org/doc/Rnews/Rnews_2006-2.pdf) a vignette for packages **distr**, **distrSim**, **distrTEst**,  
 and **distrEx** is included into the mere documentation package **distrDoc** and may be called by `require("distrDoc");vignette("distr")` a homepage to this package is available under <https://distr.r-forge.r-project.org/> M. Kohl (2005): *Numerical Contributions to the Asymptotic Theory of Robustness*. PhD Thesis. Bayreuth. Available as <https://www.stamats.de/wp-content/uploads/2018/04/ThesisMKohl.pdf>

## See Also

[distr-package](#)

AbscontCondDistribution-class  
*Absolutely continuous conditional distribution*

## Description

The class of absolutely continuous conditional univariate distributions.

## Objects from the Class

Objects can be created by calls of the form `new("AbscontCondDistribution", ...)`.

**Slots**

cond Object of class "Condition": condition  
 img Object of class "rSpace": the image space.  
 param Object of class "OptionalParameter": an optional parameter.  
 r Object of class "function": generates random numbers.  
 d Object of class "OptionalFunction": optional conditional density function.  
 p Object of class "OptionalFunction": optional conditional cumulative distribution function.  
 q Object of class "OptionalFunction": optional conditional quantile function.  
 .withArith logical: used internally to issue warnings as to interpretation of arithmetics  
 .withSim logical: used internally to issue warnings as to accuracy  
 .logExact logical: used internally to flag the case where there are explicit formulae for the log version of density, cdf, and quantile function  
 .lowerExact logical: used internally to flag the case where there are explicit formulae for the lower tail version of cdf and quantile function  
 Symmetry object of class "DistributionSymmetry"; used internally to avoid unnecessary calculations.

**Extends**

Class "UnivariateCondDistribution", directly.  
 Class "Distribution", by class "UnivariateCondDistribution".

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[UnivariateCondDistribution-class](#), [Distribution-class](#)

**Examples**

```
new("AbscontCondDistribution")
```

## Description

Generic function for the computation of asymmetric total variation distance  $d_v(\rho)$  of two distributions  $P$  and  $Q$  where the distributions may be defined for an arbitrary sample space  $(\Omega, \mathcal{A})$ . For given ratio of inlier and outlier probability  $\rho$ , this distance is defined as

$$d_v(\rho)(P, Q) = \int (dQ - c dP)_+$$

for  $c$  defined by

$$\rho \int (dQ - c dP)_+ = \int (dQ - c dP)_-$$

It coincides with total variation distance for  $\rho = 1$ .

## Usage

```
AsymTotalVarDist(e1, e2, ...)
## S4 method for signature 'AbscontDistribution,AbscontDistribution'
AsymTotalVarDist(e1,e2, rho = 1,
                 rel.tol = .Machine$double.eps^0.3, maxiter=1000, Ngrid = 10000,
                 TruncQuantile = getdistrOption("TruncQuantile"),
                 IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,DiscreteDistribution'
AsymTotalVarDist(e1,e2, rho = 1, ...)
## S4 method for signature 'DiscreteDistribution,AbscontDistribution'
AsymTotalVarDist(e1,e2, rho = 1, ...)
## S4 method for signature 'DiscreteDistribution,DiscreteDistribution'
AsymTotalVarDist(e1,e2, rho = 1, ...)
## S4 method for signature 'numeric,DiscreteDistribution'
AsymTotalVarDist(e1, e2, rho = 1, ...)
## S4 method for signature 'DiscreteDistribution,numERIC'
AsymTotalVarDist(e1, e2, rho = 1, ...)
## S4 method for signature 'numeric,AbscontDistribution'
AsymTotalVarDist(e1, e2, rho = 1, asis.smooth.discretize = "discretize",
                 n.dscr = getdistrExOption("nDiscretize"), low.dscr = getLow(e2),
                 up.dscr = getUp(e2), h.smooth = getdistrExOption("hSmooth"),
                 rel.tol = .Machine$double.eps^0.3, maxiter=1000, Ngrid = 10000,
                 TruncQuantile = getdistrOption("TruncQuantile"),
                 IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,numERIC'
AsymTotalVarDist(e1, e2, rho = 1,
                 asis.smooth.discretize = "discretize",
                 n.dscr = getdistrExOption("nDiscretize"), low.dscr = getLow(e1),
                 up.dscr = getUp(e1), h.smooth = getdistrExOption("hSmooth"),
                 rel.tol = .Machine$double.eps^0.3, maxiter=1000, Ngrid = 10000,
                 TruncQuantile = getdistrOption("TruncQuantile"),
                 IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AcDcLcDistribution,AcDcLcDistribution'
AsymTotalVarDist(e1, e2,
                 rho = 1, rel.tol = .Machine$double.eps^0.3, maxiter=1000, Ngrid = 10000,
```

```
TruncQuantile = getdistrOption("TruncQuantile"),
IQR.fac = 15, ..., diagnostic = FALSE)
```

## Arguments

e1	object of class "Distribution" or "numeric"
e2	object of class "Distribution" or "numeric"
asis.smooth.discretize	possible methods are "asis", "smooth" and "discretize". Default is "discretize".
n.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the number of lattice points used to discretize the abs. cont. distribution.
low.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the lower end point of the lattice used to discretize the abs. cont. distribution.
up.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the upper end point of the lattice used to discretize the abs. cont. distribution.
h.smooth	if asis.smooth.discretize is equal to "smooth" – i.e., the empirical distribution of the provided data should be smoothed – one has to specify this parameter.
rho	ratio of inlier/outlier radius
rel.tol	relative tolerance for distrExIntegrate and uniroot
maxiter	parameter for uniroot
Ngrid	How many grid points are to be evaluated to determine the range of the likelihood ratio?
,	
TruncQuantile	Quantile the quantile based integration bounds (see details)
IQR.fac	Factor for the scale based integration bounds (see details)
...	further arguments to be used in particular methods – (in package <b>distrEx</b> : just used for distributions with a.c. parts, where it is used to pass on arguments to <b>distrExIntegrate</b> ).
diagnostic	logical; if TRUE, the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries method ("integrate" or "GLIntegrate"), call, result (the complete return value of the method), args (the args with which the method was called), and time (the time to compute the integral).

## Details

For distances between absolutely continuous distributions, we use numerical integration; to determine sensible bounds we proceed as follows: by means of `min(getLow(e1, eps=TruncQuantile),getLow(e2, eps=TruncQuantile),max(getUp(e1, eps=TruncQuantile),getUp(e2, eps=TruncQuantile))` we determine quantile based bounds  $c(\text{low.0}, \text{up.0})$ , and by means of `s1 <- max(IQR(e1), IQR(e2)); m1 <- median(e1); m2 <- median(e2)` and `low.1 <- min(m1, m2) - s1 * IQR.fac, up.1 <- max(m1, m2) + s1 * IQR.fac` we determine scale based bounds; these are combined by `low <- max(low.0, low.1), up <- max(up.0, up.1)`.

Again in the absolutely continuous case, to determine the range of the likelihood ratio, we evaluate this ratio on a grid constructed as follows: `x.range <- c(seq(low, up, length=Ngrid/3), q.l(e1)(seq(0, 1, length=Ngrid/3)*.999), q.l(e2)(seq(0, 1, length=Ngrid/3)*.999))`

Finally, for both discrete and absolutely continuous case, we clip this ratio downwards by  $1e-10$  and upwards by  $1e10$

In case we want to compute the total variation distance between (empirical) data and an abs. cont. distribution, we can specify the parameter `asis.smooth.discretize` to avoid trivial distances (distance = 1).

Using `asis.smooth.discretize = "discretize"`, which is the default, leads to a discretization of the provided abs. cont. distribution and the distance is computed between the provided data and the discretized distribution.

Using `asis.smooth.discretize = "smooth"` causes smoothing of the empirical distribution of the provided data. This is, the empirical data is convoluted with the normal distribution `Norm(mean = 0, sd = h.smooth)` which leads to an abs. cont. distribution. Afterwards the distance between the smoothed empirical distribution and the provided abs. cont. distribution is computed.

Diagnostics on the involved integrations are available if argument `diagnostic` is TRUE. Then there is attribute `diagnostic` attached to the return value, which may be inspected and accessed through `showDiagnostic` and `getDiagnostic`.

## Value

Asymmetric Total variation distance of e1 and e2

## Methods

**e1 = "AbscontDistribution", e2 = "AbscontDistribution":** total variation distance of two absolutely continuous univariate distributions which is computed using `distrExIntegrate`.

**e1 = "AbscontDistribution", e2 = "DiscreteDistribution":** total variation distance of absolutely continuous and discrete univariate distributions (are mutually singular; i.e., have distance =1).

**e1 = "DiscreteDistribution", e2 = "DiscreteDistribution":** total variation distance of two discrete univariate distributions which is computed using `support` and `sum`.

**e1 = "DiscreteDistribution", e2 = "AbscontDistribution":** total variation distance of discrete and absolutely continuous univariate distributions (are mutually singular; i.e., have distance =1).

**e1 = "numeric", e2 = "DiscreteDistribution":** Total variation distance between (empirical) data and a discrete distribution.

**e1 = "DiscreteDistribution", e2 = "numeric":** Total variation distance between (empirical) data and a discrete distribution.

**e1 = "numeric", e2 = "AbscontDistribution":** Total variation distance between (empirical) data and an abs. cont. distribution.

**e1 = "AbscontDistribution", e1 = "numeric":** Total variation distance between (empirical) data and an abs. cont. distribution.

**e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution":** Total variation distance of mixed discrete and absolutely continuous univariate distributions.

## Author(s)

Peter Ruckdeschel <[peter.ruckdeschel@uni-oldenburg.de](mailto:peter.ruckdeschel@uni-oldenburg.de)>

## References

to be filled; Agostinelli, C and Ruckdeschel, P. (2009): A simultaneous inlier and outlier model by asymmetric total variation distance.

## See Also

[TotalVarDist-methods](#), [ContaminationSize](#), [KolmogorovDist](#), [HellingerDist](#), [Distribution-class](#)

## Examples

```
AsymTotalVarDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
    mixCoeff=c(0.2,0.8)), rho=0.3)
AsymTotalVarDist(Norm(), Td(10), rho=0.3)
AsymTotalVarDist(Norm(mean = 50, sd = sqrt(25)), Binom(size = 100), rho=0.3) # mutually singular
AsymTotalVarDist(Pois(10), Binom(size = 20), rho=0.3)

x <- rnorm(100)
AsymTotalVarDist(Norm(), x, rho=0.3)
AsymTotalVarDist(x, Norm(), asis.smooth.discretize = "smooth", rho=0.3)

y <- (rbinom(50, size = 20, prob = 0.5)-10)/sqrt(5)
AsymTotalVarDist(y, Norm(), rho=0.3)
AsymTotalVarDist(y, Norm(), asis.smooth.discretize = "smooth", rho=0.3)

AsymTotalVarDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5), rho=0.3)
```

## Condition-class

## Conditions

## Description

The class of conditions.

## Objects from the Class

Objects can be created by calls of the form `new("Condition", ...)`.

## Slots

`name` Object of class "character": name of the condition

## Methods

`name` `signature(object = "Condition")`: accessor function for slot `name`.  
`name<-` `signature(object = "Condition")`: replacement function for slot `name`.

## Author(s)

Matthias Kohl <[Matthias.Kohl@stamats.de](mailto:Matthias.Kohl@stamats.de)>

**See Also**

[UnivariateCondDistribution-class](#)

**Examples**

```
new("Condition")
```

ContaminationSize	<i>Generic Function for the Computation of the Convex Contamination (Pseudo-)Distance of Two Distributions</i>
-------------------	--

**Description**

Generic function for the computation of convex contamination (pseudo-)distance of two probability distributions  $P$  and  $Q$ . That is, the minimal size  $\varepsilon \in [0, 1]$  is computed such that there exists some probability distribution  $R$  with

$$Q = (1 - \varepsilon)P + \varepsilon R$$

**Usage**

```
ContaminationSize(e1, e2, ...)
## S4 method for signature 'AbscontDistribution,AbscontDistribution'
ContaminationSize(e1,e2)
## S4 method for signature 'DiscreteDistribution,DiscreteDistribution'
ContaminationSize(e1,e2)
## S4 method for signature 'AcDcLcDistribution,AcDcLcDistribution'
ContaminationSize(e1,e2)
```

**Arguments**

- |     |   |
|-----|---|
| e1  | object of class "Distribution"  |
| e2  | object of class "Distribution"  |
| ... | further arguments to be used in particular methods (not in package <b>distrEx</b> ) |

**Details**

Computes the distance from e1 to e2 respectively  $P$  to  $Q$ . This is not really a distance as it is not symmetric!

**Value**

A list containing the following components:

- |                       |   |
|-----------------------|---|
| e1                    | object of class "Distribution"; ideal distribution          |
| e2                    | object of class "Distribution"; 'contaminated' distribution |
| size.of.contamination | size of contamination                                       |

## Methods

- e1 = "AbscontDistribution", e2 = "AbscontDistribution":** convex contamination (pseudo-)distance of two absolutely continuous univariate distributions.
- e1 = "DiscreteDistribution", e2 = "DiscreteDistribution":** convex contamination (pseudo-)distance of two discrete univariate distributions.
- e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution":** convex contamination (pseudo-)distance of two discrete univariate distributions.

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>,  
Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

## References

Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.

## See Also

[KolmogorovDist](#), [TotalVarDist](#), [HellingerDist](#), [Distribution-class](#)

## Examples

```
ContaminationSize(Norm(), Norm(mean=0.1))
ContaminationSize(Pois(), Pois(1.5))
```

ConvexContamination     *Generic Function for Generating Convex Contaminations*

## Description

Generic function for generating convex contaminations. This is also known as *gross error model*. Given two distributions  $P$  (ideal distribution),  $R$  (contaminating distribution) and the size  $\varepsilon \in [0, 1]$  the convex contaminated distribution

$$Q = (1 - \varepsilon)P + \varepsilon R$$

is generated.

## Usage

```
ConvexContamination(e1, e2, size)
```

## Arguments

e1	object of class "Distribution": ideal distribution
e2	object of class "Distribution": contaminating distribution
size	size of contamination (amount of gross errors)

**Value**

Object of class "Distribution".

**Methods**

- e1 = "UnivariateDistribution", e2 = "UnivariateDistribution", size = "numeric":** convex combination of two univariate distributions
- e1 = "AbscontDistribution", e2 = "AbscontDistribution", size = "numeric":** convex combination of two absolutely continuous univariate distributions
- e1 = "DiscreteDistribution", e2 = "DiscreteDistribution", size = "numeric":** convex combination of two discrete univariate distributions
- e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution", size = "numeric":** convex combination of two univariate distributions which may be coerced to "UnivarLebDecDistribution".

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**References**

Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.

**See Also**

[ContaminationSize, Distribution-class](#)

**Examples**

```
# Convex combination of two normal distributions
C1 <- ConvexContamination(e1 = Norm(), e2 = Norm(mean = 5), size = 0.1)
plot(C1)
```

CvMDist

*Generic function for the computation of the Cramer - von Mises distance of two distributions*

**Description**

Generic function for the computation of the Cramer - von Mises distance  $d_\mu$  of two distributions  $P$  and  $Q$  where the distributions are defined on a finite-dimensional Euclidean space  $(\mathbb{R}^m, \mathcal{B}^m)$  with  $\mathcal{B}^m$  the Borel- $\sigma$ -algebra on  $\mathbb{R}^m$ . The Cramer - von Mises distance is defined as

$$d_\mu(P, Q)^2 = \int (P(\{y \in \mathbb{R}^m \mid y \leq x\}) - Q(\{y \in \mathbb{R}^m \mid y \leq x\}))^2 \mu(dx)$$

where  $\leq$  is coordinatewise on  $\mathbb{R}^m$ .

## Usage

```
CvMDist(e1, e2, ...)
## S4 method for signature 'UnivariateDistribution,UnivariateDistribution'
CvMDist(e1, e2, mu = e1, useApply = FALSE, ..., diagnostic = FALSE)
## S4 method for signature 'numeric,UnivariateDistribution'
CvMDist(e1, e2, mu = e1, ..., diagnostic = FALSE)
```

## Arguments

e1	object of class "Distribution" or class "numeric"
e2	object of class "Distribution"
...	further arguments to be used e.g. by E()
useApply	logical; to be passed to E()
mu	object of class "Distribution"; integration measure; defaulting to e2
diagnostic	logical; if TRUE, the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries method ("integrate" or "GLIntegrate"), call, result (the complete return value of the method), args (the args with which the method was called), and time (the time to compute the integral).

## Details

Diagnostics on the involved integrations are available if argument `diagnostic` is TRUE. Then there is attribute `diagnostic` attached to the return value, which may be inspected and accessed through `showDiagnostic` and `getDiagnostic`.

## Value

Cramer - von Mises distance of e1 and e2

## Methods

- e1 = "UnivariateDistribution", e2 = "UnivariateDistribution":** Cramer - von Mises distance of two univariate distributions.
- e1 = "numeric", e2 = "UnivariateDistribution":** Cramer - von Mises distance between the empirical formed from a data set (e1) and a univariate distribution.

## Author(s)

Matthias Kohl <[Matthias.Kohl@stamats.de](mailto:Matthias.Kohl@stamats.de)>,  
Peter Ruckdeschel <[peter.ruckdeschel@uni-oldenburg.de](mailto:peter.ruckdeschel@uni-oldenburg.de)>

## References

Rieder, H. (1994) *Robust Asymptotic Statistics*. New York: Springer.

**See Also**

[ContaminationSize](#), [TotalVarDist](#), [HellingerDist](#), [KolmogorovDist](#), [Distribution-class](#)

**Examples**

```
CvMDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
                                         mixCoeff=c(0.2,0.8)))
CvMDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
                                         mixCoeff=c(0.2,0.8)),mu=Norm())
CvMDist(Norm(), Td(10))
CvMDist(Norm(mean = 50, sd = sqrt(25)), Binom(size = 100))
CvMDist(Pois(10), Binom(size = 20))
CvMDist(rnorm(100),Norm())
CvMDist((rbinom(50, size = 20, prob = 0.5)-10)/sqrt(5), Norm())
CvMDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5))
CvMDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5), mu = Pois())
```

[dim-methods](#)

*Methods for Function dim in Package ‘distrEx’*

**Description**

[dim-methods](#)

**Methods**

**dim** `signature(object = "DiscreteMVDistribution")`: returns the dimension of the distribution

**See Also**

[dim-methods](#),  
[dim](#)

[DiscreteCondDistribution-class](#)

*Discrete conditional distribution*

**Description**

The class of discrete conditional univariate distributions.

**Objects from the Class**

Objects can be created by calls of the form `new("DiscreteCondDistribution", ...)`.

**Slots**

support Object of class "function": conditional support.  
 cond Object of class "Condition": condition  
 img Object of class "rSpace": the image space.  
 param Object of class "OptionalParameter": an optional parameter.  
 r Object of class "function": generates random numbers.  
 d Object of class "OptionalFunction": optional conditional density function.  
 p Object of class "OptionalFunction": optional conditional cumulative distribution function.  
 q Object of class "OptionalFunction": optional conditional quantile function.  
 .withArith logical: used internally to issue warnings as to interpretation of arithmetics  
 .withSim logical: used internally to issue warnings as to accuracy  
 .logExact logical: used internally to flag the case where there are explicit formulae for the log version of density, cdf, and quantile function  
 .lowerExact logical: used internally to flag the case where there are explicit formulae for the lower tail version of cdf and quantile function  
 Symmetry object of class "DistributionSymmetry"; used internally to avoid unnecessary calculations.

**Extends**

Class "UnivariateCondDistribution", directly.  
 Class "Distribution", by class "UnivariateCondDistribution".

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[UnivariateCondDistribution-class](#)

**Examples**

```
new("DiscreteCondDistribution")
```

**DiscreteMVDistribution***Generating function for multivariate discrete distribution***Description**

Generates an object of class "DiscreteMVDistribution".

**Usage**

```
DiscreteMVDistribution(supp, prob, Symmetry = NoSymmetry())
```

**Arguments**

- |          |  |
|----------|--|
| supp     | numeric matrix whose rows form the support of the discrete multivariate distribution.  |
| prob     | vector of probability weights for the elements of supp.  |
| Symmetry | you may help R in calculations if you tell it whether the distribution is non-symmetric (default) or symmetric with respect to a center. |

**Details**

Typical usages are

```
DiscreteMVDistribution(supp, prob)
DiscreteMVDistribution(supp)
```

Identical rows are collapsed to unique support values. If prob is missing, all elements in supp are equally weighted.

**Value**

Object of class "DiscreteMVDistribution"

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[DiscreteMVDistribution-class](#)

## Examples

```
# Dirac-measure at (0,0,0)
D1 <- DiscreteMVDistribution(supp = c(0,0,0))
support(D1)

# simple discrete distribution
D2 <- DiscreteMVDistribution(supp = matrix(c(0,1,0,2,2,1,1,0), ncol=2),
                             prob = c(0.3, 0.2, 0.2, 0.3))
support(D2)
r(D2)(10)
```

## DiscreteMVDistribution-class

*Discrete Multivariate Distributions*

## Description

The class of discrete multivariate distributions.

## Objects from the Class

Objects can be created by calls of the form `new("DiscreteMVDistribution", ...)`. More frequently they are created via the generating function `DiscreteMVDistribution`.

## Slots

- `img` Object of class "rSpace". Image space of the distribution. Usually an object of class "EuclideanSpace".
- `param` Object of class "OptionalParameter". Optional parameter of the multivariate distribution.
- `r` Object of class "function": generates (pseudo-)random numbers
- `d` Object of class "OptionalFunction": optional density function
- `p` Object of class "OptionalFunction": optional cumulative distribution function
- `q` Object of class "OptionalFunction": optional quantile function
- `support` numeric matrix whose rows form the support of the distribution
- `.finSupport` logical: (later on to be) used internally to check whether the true support is finite; the element in the 1st row and  $i$ th column indicates whether the  $i$ th marginal distribution has a finite left endpoint, and the element in the 2nd row and  $i$ th column if it is has a finite right endpoint); not yet further used.
- `.withArith` logical: used internally to issue warnings as to interpretation of arithmetics
- `.withSim` logical: used internally to issue warnings as to accuracy
- `.logExact` logical: used internally to flag the case where there are explicit formulae for the log version of density, cdf, and quantile function
- `.lowerExact` logical: used internally to flag the case where there are explicit formulae for the lower tail version of cdf and quantile function

**Extends**

Class "MultivariateDistribution", directly.  
 Class "Distribution", by class "MultivariateDistribution".

**Methods**

**support** `signature(object = "DiscreteMVDistribution")`: accessor function for slot support.

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[Distribution-class](#), [MultivariateDistribution-class](#), [DiscreteMVDistribution](#), [E-methods](#)

**Examples**

```
(D1 <- new("MultivariateDistribution")) # Dirac measure in (0,0)
r(D1)(5)

(D2 <- DiscreteMVDistribution(supp = matrix(c(1:5, rep(3, 5)), ncol=2, byrow=TRUE)))
support(D2)
r(D2)(10)
d(D2)(support(D2))
p(D2)(lower = c(1,1), upper = c(3,3))
q(D2)
## in RStudio or Jupyter IRKernel, use q.l(.)() instead of q(.)()
param(D2)
img(D2)

e1 <- E(D2) # expectation
```

**Description**

Numerical integration via `integrate`. In case `integrate` fails a Gauss-Legendre quadrature is performed.

**Usage**

```
distrExIntegrate(f, lower, upper, subdivisions = 100,
                  rel.tol = .Machine$double.eps^0.25,
                  abs.tol = rel.tol, stop.on.error = TRUE,
                  distr, order, ..., diagnostic = FALSE)
showDiagnostic(x, what, withNonShows = FALSE, ...)
```

```
getDiagnostic(x, what, reorganized=TRUE)
## S3 method for class 'DiagnosticClass'
print(x, what, withNonShows = FALSE, xname, ...)
```

## Arguments

<code>f</code>	an R function taking a numeric first argument and returning a numeric vector of the same length. Returning a non-finite element will generate an error.
<code>lower</code>	lower limit of integration. Can be <code>-Inf</code> .
<code>upper</code>	upper limit of integration. Can be <code>Inf</code> .
<code>subdivisions</code>	the maximum number of subintervals.
<code>rel.tol</code>	relative accuracy requested.
<code>abs.tol</code>	absolute accuracy requested.
<code>stop.on.error</code>	logical. If <code>TRUE</code> (the default) an error stops the function. If <code>false</code> some errors will give a result with a warning in the <code>message</code> component.
<code>distr</code>	object of class <code>UnivariateDistribution</code> .
<code>order</code>	order of Gauss-Legendre quadrature.
<code>diagnostic</code>	logical; if <code>TRUE</code> , the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries <code>method</code> ("integrate" or "GLIntegrate"), <code>call</code> , <code>result</code> (the complete return value of the method), <code>args</code> (the args with which the method was called), and <code>time</code> (the time to compute the integral).
<code>...</code>	In case of integrators: additional arguments to be passed to <code>f</code> . Remember to use argument names not matching those of <code>integrate</code> and <code>GLIntegrate</code> ! In case of <code>showDiagnostic</code> , <code>print.DiagnosticClass</code> : additional arguments to be passed on to print methods called for particular items in the diagnostic list.
<code>x</code>	the item for which the diagnostic is to be shown.
<code>what</code>	a character vector with all the diagnostic items to be selected/shown. If empty or missing all items are selected/shown.
<code>withNonShows</code>	internally we distinguish items which are easily printed (first kind) (numeric, logical, character) and more difficult ones (second kind), e.g., calls, functions, lists. The distinction is made according to the list item name. If <code>withNonShows==TRUE</code> one also attempts to show the selected items of the second kind, otherwise they are not shown (but returned).
<code>xname</code>	an optional name for the diagnostic object to be shown.
<code>reorganized</code>	should the diagnostic information be reorganized (using internal function <code>.reorganizeDiagnosticList?</code> )

## Details

`distrExIntegrate` calls `integrate`. In case `integrate` returns an error a Gauss-Legendre integration is performed using `GLIntegrate`. If `lower` or (and) `upper` are infinite the `GLIntegrateTruncQuantile`, respectively the `1-GLIntegrateTruncQuantile` quantile of `distr` is used instead.

`distrExIntegrate` is called from many places in the `distr` and `robust` families of packages. At every such instance, diagnostic information can be collected (setting a corresponding argument

`diagnostic` to TRUE in the calling function. This diagnostic information is originally stored in a tree like list structure of S3 class `DiagnosticClass` which is then attached as attribute `diagnostic` to the respective object. It can be inspected and accessed through `showDiagnostic` and `getDiagnostic`. More specifically, for any object with attribute `diagnostic`, `showDiagnostic` shows the diagnostic collected during integration, and `getDiagnostic` returns the diagnostic collected during integration. To this end, `print.DiagnosticClass` is an S3 method for `print` for objects of S3 class `DiagnosticClass`.

### Value

The value of `distrExIntegrate` is a numeric approximation of the integral. If argument `diagnostic==TRUE` in `distrExIntegrate`, the return value has an attribute `diagnostic` of S3 class `DiagnosticClass` containing diagnostic information on the integration.

`showDiagnostic`, `getDiagnostic`, `print.DiagnosticClass` all return (invisibly) a list with the selected items, reorganized by internal function `.reorganizeDiagnosticList`, respectively, in case of argument `reorganized==FALSE`, `getDiagnostic` returns (invisibly) the diagnostic information as is.

### Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

### References

Based on QUADPACK routines dqags and dqagi by R. Piessens and E. deDoncker-Kapenga, available from Netlib.

R. Piessens, E. deDoncker-Kapenga, C. Uberhuber, D. Kahaner (1983) *Quadpack: a Subroutine Package for Automatic Integration*. Springer Verlag.

W.H. Press, S.A. Teukolsky, W.T. Vetterling, B.P. Flannery (1992) *Numerical Recipies in C. The Art of Scientific Computing*. Second Edition. Cambridge University Press.

### See Also

[integrate](#), [GLIntegrate](#), [distrExOptions](#)

### Examples

```
fkt <- function(x){x*dchisq(x+1, df = 1)}
integrate(fkt, lower = -1, upper = 3)
GLIntegrate(fkt, lower = -1, upper = 3)
try(integrate(fkt, lower = -1, upper = 5))
distrExIntegrate(fkt, lower = -1, upper = 5)
```

---

distrExMASK*Masking of/by other functions in package "distrEx"*

---

**Description**

Provides information on the (intended) masking of and (non-intended) masking by other other functions in package **distrEx**

**Usage**

```
distrExMASK(library = NULL)
```

**Arguments**

library	a character vector with path names of R libraries, or NULL. The default value of NULL corresponds to all libraries currently known. If the default is used, the loaded packages are searched before the libraries
---------	---

**Value**

no value is returned

**Author(s)**

Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

**Examples**

```
## IGNORE_RDIFF_BEGIN
distrExMASK()
## IGNORE_RDIFF_END
```

---

distrExMOVED

*Moved functionality from package "distrEx"*

---

**Description**

Provides information on moved of functionality from package **distrEx**.

**Usage**

```
distrExMOVED(library = NULL)
```

**Arguments**

library	a character vector with path names of R libraries, or NULL. The default value of NULL corresponds to all libraries currently known. If the default is used, the loaded packages are searched before the libraries
---------	---

**Value**

no value is returned

**Author(s)**

Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

**Examples**

```
## IGNORE_RDIFF_BEGIN
distrExMOVED()
## IGNORE_RDIFF_END
```

**distrExOptions**

*Function to change the global variables of the package ‘distrEx’*

**Description**

With **distrExOptions** you can inspect and change the global variables of the package **distrEx**.

**Usage**

```
distrExOptions(...)
distrExOptions(...)
getdistrExOption(x)
```

**Arguments**

- ... any options can be defined, using name = value or by passing a list of such tagged values.
- x a character string holding an option name.

**Value**

**distrExOptions()** returns a list of the global variables.  
**distrExOptions(x)** returns the global variable x.  
**getdistrExOption(x)** returns the global variable x.  
**distrExOptions(x=y)** sets the value of the global variable x to y.

**distrExOptions**

For compatibility with spelling in package **distr**, **distrExOptions** is just a synonym to **distrExOptions**.

## Global Options

**MCIterations:** number of Monte-Carlo iterations used for crude Monte-Carlo integration; defaults to 1e5.

**GLIntegrateTruncQuantile:** If integrate fails and there are infinite integration limits, the function GLIntegrate is called inside of distrExIntegrate with the corresponding quantiles GLIntegrateTruncQuantile respectively, 1 - GLIntegrateTruncQuantile as finite integration limits; defaults to 10\*.Machine\$double.eps.

**GLIntegrateOrder:** The order used for the Gauss-Legendre integration inside of distrExIntegrate; defaults to 500.

**ElowerTruncQuantile:** The lower limit of integration used inside of E which corresponds to the ElowerTruncQuantile-quantile; defaults to 1e-7.

**EupperTruncQuantile:** The upper limit of integration used inside of E which corresponds to the (1-ElowerTruncQuantile)-quantile; defaults to 1e-7.

**ErelativeTolerance:** The relative tolerance used inside of E when calling distrExIntegrate; defaults to .Machine\$double.eps^0.25.

**m1dfLowerTruncQuantile:** The lower limit of integration used inside of m1df which corresponds to the m1dfLowerTruncQuantile-quantile; defaults to 0.

**m1dfRelativeTolerance:** The relative tolerance used inside of m1df when calling distrExIntegrate; defaults to .Machine\$double.eps^0.25.

**m2dfLowerTruncQuantile:** The lower limit of integration used inside of m2df which corresponds to the m2dfLowerTruncQuantile-quantile; defaults to 0.

**m2dfRelativeTolerance:** The relative tolerance used inside of m2df when calling distrExIntegrate; defaults to .Machine\$double.eps^0.25.

**nDiscretize:** number of support values used for the discretization of objects of class "AbscontDistribution"; defaults to 100.

**hSmooth:** smoothing parameter to smooth objects of class "DiscreteDistribution". This is done via convolution with the normal distribution Norm(mean = 0, sd = hSmooth); defaults to 0.05.

**IQR.fac:** for determining sensible integration ranges, we use both quantile and scale based methods; for the scale based method we use the median of the distribution  $\pm$  IQR.fac  $\times$  the IQR; defaults to 15.

**propagate.names.functionals** should names obtained from parameter coordinates be propagated to return values of specific S4 methods for functionals; defaults to TRUE.

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## See Also

[options](#), [getOption](#)

## Examples

```
distrExOptions()
distrExOptions("ElowerTruncQuantile")
distrExOptions("ElowerTruncQuantile" = 1e-6)
# or
distrExOptions(ElowerTruncQuantile = 1e-6)
getdistrExOption("ElowerTruncQuantile")
```

## Description

Generic function for the computation of (conditional) expectations.

## Usage

```
E(object, fun, cond, ...)

## S4 method for signature 'UnivariateDistribution,missing,missing'
E(object,
  low = NULL, upp = NULL, Nsim = getdistrExOption("MCIterations"), ...)

## S4 method for signature 'UnivariateDistribution,function,missing'
E(object, fun,
  useApply = TRUE, low = NULL, upp = NULL,
  Nsim = getdistrExOption("MCIterations"), ...)

## S4 method for signature 'AbscontDistribution,missing,missing'
E(object, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'AbscontDistribution,function,missing'
E(object, fun, useApply = TRUE,
  low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'UnivarMixingDistribution,missing,missing'
E(object, low = NULL,
  upp = NULL, rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
```

```

upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'UnivarMixingDistribution,function,missing'
E(object, fun,
  useApply = TRUE, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'UnivarMixingDistribution,missing,ANY'
E(object, cond, low = NULL,
  upp = NULL, rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'UnivarMixingDistribution,function,ANY'
E(object, fun, cond,
  useApply = TRUE, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'DiscreteDistribution,function,missing'
E(object, fun, useApply = TRUE,
  low = NULL, upp = NULL, ...)

## S4 method for signature 'AffLinDistribution,missing,missing'
E(object, low = NULL, upp = NULL,
  ..., diagnostic = FALSE)

## S4 method for signature 'AffLinUnivarLebDecDistribution,missing,missing'
E(object, low = NULL,
  upp = NULL, ..., diagnostic = FALSE)

## S4 method for signature 'MultivariateDistribution,missing,missing'
E(object,
  Nsim = getdistrExOption("MCIterations"), ...)
## S4 method for signature 'MultivariateDistribution,function,missing'
E(object, fun,
  useApply = TRUE, Nsim = getdistrExOption("MCIterations"), ...)

## S4 method for signature 'DiscreteMVDistribution,missing,missing'
E(object, low = NULL,
  upp = NULL, ...)

```

```

## S4 method for signature 'DiscreteMVDistribution,function,missing'
E(object, fun,
  useApply = TRUE, ...)

## S4 method for signature 'AbscontCondDistribution,missing,numERIC'
E(object, cond,
  useApply = TRUE, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)

## S4 method for signature 'DiscreteCondDistribution,missing,numERIC'
E(object, cond,
  useApply = TRUE, low = NULL, upp = NULL, ...)

## S4 method for signature 'UnivariateCondDistribution,function,numERIC'
E(object, fun, cond,
  withCond = FALSE, useApply = TRUE, low = NULL, upp = NULL,
  Nsim = getdistrExOption("MCIterations"), ...)

## S4 method for signature 'AbscontCondDistribution,function,numERIC'
E(object, fun, cond,
  withCond = FALSE, useApply = TRUE, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"),
  , ..., diagnostic = FALSE)

## S4 method for signature 'DiscreteCondDistribution,function,numERIC'
E(object, fun, cond,
  withCond = FALSE, useApply = TRUE, low = NULL, upp = NULL,...)

## S4 method for signature 'UnivarLebDecDistribution,missing,missing'
E(object, low = NULL,
  upp = NULL, rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE )

## S4 method for signature 'UnivarLebDecDistribution,function,missing'
E(object, fun,
  useApply = TRUE, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE )

```

```

## S4 method for signature 'UnivarLebDecDistribution,missing,ANY'
E(object, cond, low = NULL,
  upp = NULL, rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE )
## S4 method for signature 'UnivarLebDecDistribution,function,ANY'
E(object, fun, cond,
  useApply = TRUE, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE )

## S4 method for signature 'AcDcLcDistribution,ANY,ANY'
E(object, fun, cond, low = NULL,
  upp = NULL, rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = getdistrExOption("IQR.fac"), ..., diagnostic = FALSE)
## S4 method for signature 'CompoundDistribution,missing,missing'
E(object, low = NULL,
  upp = NULL, ..., diagnostic = FALSE)

## S4 method for signature 'Arcsine,missing,missing'
E(object, low = NULL, upp = NULL, ..., diagnostic = FALSE)
## S4 method for signature 'Beta,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Binom,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Cauchy,missing,missing'
E(object, low = NULL, upp = NULL, ..., diagnostic = FALSE)
## S4 method for signature 'Cauchy,function,missing'
E(object, fun, low = NULL, upp = NULL,
  rel.tol = getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = max(1e4,getdistrExOption("IQR.fac")),
  ..., diagnostic = FALSE)
## S4 method for signature 'Chisq,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Dirac,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)

```

```

## S4 method for signature 'DExp,missing,missing'
E(object, low = NULL, upp = NULL, ..., diagnostic = FALSE)
## S4 method for signature 'Exp,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Fd,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Gammad,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Gammad,function,missing'
E(object, fun, low = NULL, upp = NULL,
  rel.tol = getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = max(1e4,getdistrExOption("IQR.fac")), ..., diagnostic = FALSE)
## S4 method for signature 'Geom,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Hyper,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Logis,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Lnorm,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Nbinom,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Norm,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Pois,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Unif,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Td,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...)
```

```

propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Weibull,missing,missing'
E(object, low = NULL, upp = NULL,
  propagate.names=getdistrExOption("propagate.names.functionals"), ...,
  diagnostic = FALSE)
## S4 method for signature 'Weibull,function,missing'
E(object, fun, low = NULL, upp = NULL,
  rel.tol = getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = max(1e4,getdistrExOption("IQR.fac")), ..., diagnostic = FALSE)
.qtlIntegrate(object, fun, low = NULL, upp = NULL,
  rel.tol= getdistrExOption("ErelativeTolerance"),
  lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
  upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
  IQR.fac = max(1e4,getdistrExOption("IQR.fac")), ...,
  .withLeftTail = FALSE, .withRightTail = FALSE, diagnostic = FALSE)

```

## Arguments

<code>object</code>	object of class "Distribution"
<code>fun</code>	if missing the (conditional) expectation is computed else the (conditional) expectation of <code>fun</code> is computed.
<code>cond</code>	if not missing the conditional expectation given <code>cond</code> is computed.
<code>Nsim</code>	number of MC simulations used to determine the expectation.
<code>rel.tol</code>	relative tolerance for <code>distrExIntegrate</code> .
<code>low</code>	lower bound of integration range.
<code>upp</code>	upper bound of integration range.
<code>lowerTruncQuantile</code>	lower quantile for quantile based integration range.
<code>upperTruncQuantile</code>	upper quantile for quantile based integration range.
<code>IQR.fac</code>	factor for scale based integration range (i.e.; median of the distribution $\pm$ <code>IQR.fac</code> $\times$ IQR).
<code>...</code>	additional arguments to <code>fun</code>
<code>useApply</code>	logical: should <code>sapply</code> , respectively <code>apply</code> be used to evaluate <code>fun</code> .
<code>withCond</code>	logical: is <code>cond</code> in the argument list of <code>fun</code> .
<code>.withLeftTail</code>	logical: should left tail (falling into quantile range [0,0.02]) be computed separately to enhance accuracy?
<code>.withRightTail</code>	logical: should right tail (falling into quantile range [0.98,1]) be computed separately to enhance accuracy?
<code>diagnostic</code>	logical; if TRUE, the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries <code>method</code> ("integrate" or "GLIntegrate"), <code>call</code> , <code>result</code> (the complete return value of the method), <code>args</code> (the args with which the method was called), and <code>time</code> (the time to compute the integral).

`propagate.names`

logical: should names obtained from parameter coordinates be propagated to return values of specific S4 methods for functionals; defaults to the value of the respective `distrExoption propagate.names.functionals`.

## Details

The precision of the computations can be controlled via certain global options; cf. [distrExOptions](#). Also note that arguments `low` and `upp` should be given as named arguments in order to prevent them to be matched by arguments `fun` or `cond`. Also the result, when arguments `low` or `upp` is given, is the *unconditional value* of the expectation; no conditioning with respect to `low <= object <= upp` is done.

For the Cauchy, the Gamma and Weibull distribution for integration with missing argument `cond` but given argument `fun`, we use integration on  $[0,1]$  (i.e., via the respective probability transformation). This done via helper function `.qtlIntegrate`, where both arguments `.withLeftTail` and `.withRightTail` are `TRUE` for the Cauchy and Gamma distributions, and only `.withRightTail` is `TRUE` for the Weibull distribution.

Diagnostics on the involved integrations are available if argument `diagnostic` is `TRUE`. Then there is attribute `diagnostic` attached to the return value, which may be inspected and accessed through `showDiagnostic` and `getDiagnostic`.

## Value

The (conditional) expectation is computed.

## Methods

- `object = "UnivariateDistribution", fun = "missing", cond = "missing"`: expectation of univariate distributions using crude Monte-Carlo integration.
- `object = "AbscontDistribution", fun = "missing", cond = "missing"`: expectation of absolutely continuous univariate distributions using `distrExIntegrate`.
- `object = "DiscreteDistribution", fun = "missing", cond = "missing"`: expectation of discrete univariate distributions using `support` and `sum`.
- `object = "MultivariateDistribution", fun = "missing", cond = "missing"`: expectation of multivariate distributions using crude Monte-Carlo integration.
- `object = "DiscreteMVDistribution", fun = "missing", cond = "missing"`: expectation of discrete multivariate distributions. The computation is based on `support` and `sum`.
- `object = "UnivariateDistribution", fun = "missing", cond = "missing"`: expectation of univariate Lebesgue decomposed distributions by separate calculations for discrete and absolutely continuous part.
- `object = "AffLinDistribution", fun = "missing", cond = "missing"`: expectation of an affine linear transformation  $aX+b$  as  $aE[X]+b$  for  $X$  either `"DiscreteDistribution"` or `"AbscontDistribution"`.
- `object = "AffLinUnivarLebDecDistribution", fun = "missing", cond = "missing"`: expectation of an affine linear transformation  $aX+b$  as  $aE[X]+b$  for  $X$  either `"UnivarLebDecDistribution"`.
- `object = "UnivariateDistribution", fun = "function", cond = "missing"`: expectation of `fun` under univariate distributions using crude Monte-Carlo integration.

**object = "UnivariateDistribution", fun = "function", cond = "missing":** expectation of fun under univariate Lebesgue decomposed distributions by separate calculations for discrete and absolutely continuous part.

**object = "AbscontDistribution", fun = "function", cond = "missing":** expectation of fun under absolutely continuous univariate distributions using distrExIntegrate.

**object = "DiscreteDistribution", fun = "function", cond = "missing":** expectation of fun under discrete univariate distributions using support and sum.

**object = "MultivariateDistribution", fun = "function", cond = "missing":** expectation of multivariate distributions using crude Monte-Carlo integration.

**object = "DiscreteMVDistribution", fun = "function", cond = "missing":** expectation of fun under discrete multivariate distributions. The computation is based on support and sum.

**object = "UnivariateCondDistribution", fun = "missing", cond = "numeric":** conditional expectation for univariate conditional distributions given cond. The integral is computed using crude Monte-Carlo integration.

**object = "AbscontCondDistribution", fun = "missing", cond = "numeric":** conditional expectation for absolutely continuous, univariate conditional distributions given cond. The computation is based on distrExIntegrate.

**object = "DiscreteCondDistribution", fun = "missing", cond = "numeric":** conditional expectation for discrete, univariate conditional distributions given cond. The computation is based on support and sum.

**object = "UnivariateCondDistribution", fun = "function", cond = "numeric":** conditional expectation of fun under univariate conditional distributions given cond. The integral is computed using crude Monte-Carlo integration.

**object = "AbscontCondDistribution", fun = "function", cond = "numeric":** conditional expectation of fun under absolutely continuous, univariate conditional distributions given cond. The computation is based on distrExIntegrate.

**object = "DiscreteCondDistribution", fun = "function", cond = "numeric":** conditional expectation of fun under discrete, univariate conditional distributions given cond. The computation is based on support and sum.

**object = "UnivarLebDecDistribution", fun = "missing", cond = "missing":** expectation by separate evaluation of expectation of discrete and abs. continuous part and subsequent weighting.

**object = "UnivarLebDecDistribution", fun = "function", cond = "missing":** expectation by separate evaluation of expectation of discrete and abs. continuous part and subsequent weighting.

**object = "UnivarLebDecDistribution", fun = "missing", cond = "ANY":** expectation by separate evaluation of expectation of discrete and abs. continuous part and subsequent weighting.

**object = "UnivarLebDecDistribution", fun = "function", cond = "ANY":** expectation by separate evaluation of expectation of discrete and abs. continuous part and subsequent weighting.

**object = "UnivarMixingDistribution", fun = "missing", cond = "missing":** expectation is computed component-wise with subsequent weighting acc. to mixCoeff.

**object = "UnivarMixingDistribution", fun = "function", cond = "missing":** expectation is computed component-wise with subsequent weighting acc. to mixCoeff.

**object = "UnivarMixingDistribution", fun = "missing", cond = "ANY":** expectation is computed component-wise with subsequent weighting acc. to mixCoeff.

**object = "UnivarMixingDistribution", fun = "function", cond = "ANY":** expectation is computed component-wise with subsequent weighting acc. to mixCoeff.

**object = "AcDcLcDistribution", fun = "ANY", cond = "ANY":** expectation by first coercing to class "UnivarLebDecDistribution" and using the corresponding method.

**object = "CompoundDistribution", fun = "missing", cond = "missing":** if we are in i.i.d. situation (i.e., slot SummandsDistr is of class UnivariateDistribution) the formula  $E[N]E[S]$  for  $N$  the frequency distribution and  $S$  the summand distribution; else we coerce to "UnivarLebDecDistribution".

**object = "Arcsine", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Beta", fun = "missing", cond = "missing":** for noncentrality 0 exact evaluation using explicit expressions.

**object = "Binom", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Cauchy", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Chisq", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Dirac", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "DExp", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Exp", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Fd", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Gammad", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Gammad", fun = "function", cond = "missing":** use integration over the quantile range for numerical integration via helper function .qt1Integrate.

**object = "Geom", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Hyper", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Logis", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Lnorm", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Nbinom", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Norm", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Pois", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Unif", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Td", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Weibull", fun = "missing", cond = "missing":** exact evaluation using explicit expressions.

**object = "Weibull", fun = "function", cond = "missing":** use integration over the quantile range for numerical integration via helper function .qt1Integrate.

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de> and Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

## See Also

[distrExIntegrate](#), [m1df](#), [m2df](#), [Distribution-class](#)

## Examples

```
# mean of Exp(1) distribution
E <- Exp()

E(E) ## uses explicit terms
E(as(E,"AbscontDistribution")) ## uses numerical integration
E(as(E,"UnivariateDistribution")) ## uses simulations
E(E, fun = function(x){2*x^2}) ## uses simulations

# the same operator for discrete distributions:
P <- Pois(lambda=2)

E(P) ## uses explicit terms
E(as(P,"DiscreteDistribution")) ## uses sums
E(as(P,"UnivariateDistribution")) ## uses simulations
E(P, fun = function(x){2*x^2}) ## uses simulations

# second moment of N(1,4)
E(Norm(mean=1, sd=2), fun = function(x){x^2})
E(Norm(mean=1, sd=2), fun = function(x){x^2}, useApply = FALSE)

# conditional distribution of a linear model
D1 <- LMCondDistribution(theta = 1)
E(D1, cond = 1)
E(Norm(mean=1))
E(D1, function(x){x^2}, cond = 1)
E(Norm(mean=1), fun = function(x){x^2})
E(D1, function(x, cond){cond*x^2}, cond = 2, withCond = TRUE, useApply = FALSE)
E(Norm(mean=2), function(x){2*x^2})

E(as(Norm(mean=2),"AbscontDistribution"))
### somewhat less accurate:
E(as(Norm(mean=2),"AbscontDistribution"),
  lowerTruncQuantil=1e-4,upperTruncQuantil=1e-4, IQR.fac= 4)
### even less accurate:
E(as(Norm(mean=2),"AbscontDistribution"),
  lowerTruncQuantil=1e-2,upperTruncQuantil=1e-2, IQR.fac= 4)
### no good idea, but just as an example:
E(as(Norm(mean=2),"AbscontDistribution"),
  lowerTruncQuantil=1e-2,upperTruncQuantil=1e-2, IQR.fac= .1)

### truncation of integration range; see also m1df...
E(Norm(mean=2), low=2, upp=4)
```

```
E(Cauchy())
E(Cauchy(), upp=3, low=-2)
# some Lebesgue decomposed distribution
mymix <- UnivarLebDecDistribution(acPart = Norm(), discretePart = Binom(4,.4),
                                    acWeight = 0.4)
E(mymix)
```

**EmpiricalMVDistribution***Generating function for multivariate discrete distribution***Description**

Generates an object of class "DiscreteMVDistribution".

**Usage**

```
EmpiricalMVDistribution(data, Symmetry = NoSymmetry())
```

**Arguments**

- |          |  |
|----------|--|
| data     | numeric matrix with data where the rows are interpreted as observations.   |
| Symmetry | you may help R in calculations if you tell it whether the distribution is non-symmetric (default) or symmetric with respect to a center. |

**Details**

The function is a simple utility function providing a wrapper to the generating function [DiscreteMVDistribution](#).

Typical usages are

```
EmpiricalMVDistribution(data)
```

Identical rows are collapsed to unique support values. If prob is missing, all elements in supp are equally weighted.

**Value**

Object of class "DiscreteMVDistribution"

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[DiscreteMVDistribution](#)

**Examples**

```
## generate some data
X <- matrix(rnorm(50), ncol = 5)

## empirical distribution of X
D1 <- EmpiricalMVDistribution(data = X)
support(D1)
r(D1)(10)
```

---

EuclCondition      *Generating function for EuclCondition-class*

---

**Description**

Generates an object of class "EuclCondition".

**Usage**

```
EuclCondition(dimension)
```

**Arguments**

dimension      positive integer: dimension of the Euclidean space

**Value**

Object of class "EuclCondition"

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[EuclCondition-class](#)

**Examples**

```
EuclCondition(dimension = 3)

## The function is currently defined as
function(dimension){
  new("EuclCondition", Range = EuclideanSpace(dimension = dimension))
}
```

---

**EuclCondition-class**     *Conditioning by an Euclidean space.*

---

## Description

Conditioning by an Euclidean space.

## Objects from the Class

Objects can be created by calls of the form `new("EuclCondition", ...)`. More frequently they are created via the generating function `EuclCondition`.

## Slots

**Range** Object of class "EuclideanSpace".

**name** Object of class "character": name of condition.

## Extends

Class "Condition", directly.

## Methods

**Range** `signature(object = "EuclCondition")` accessor function for slot Range.

**show** `signature(object = "EuclCondition")`

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## See Also

[Condition-class](#), [EuclCondition](#)

## Examples

```
new("EuclCondition")
```

---

GLIntegrate	Gauss-Legendre Quadrature
-------------	---------------------------

---

## Description

Gauss-Legendre quadrature over a finite interval.

## Usage

```
GLIntegrate(f, lower, upper, order = 500, ...)
```

## Arguments

f	an R function taking a numeric first argument and returning a numeric vector of the same length. Returning a non-finite element will generate an error.
lower	finite lower limit of integration.
upper	finite upper limit of integration.
order	order of Gauss-Legendre quadrature.
...	additional arguments to be passed to f. Remember to use argument names not matching those of GLIntegrate!

## Details

In case `order = 100, 500, 1000` saved abscissas and weights are used. Otherwise the corresponding abscissas and weights are computed using the algorithm given in Section 4.5 of Press et al. (1992).

## Value

Estimate of the integral.

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## References

W.H. Press, S.A. Teukolsky, W.T. Vetterling, B.P. Flannery (1992) *Numerical Recipes in C. The Art of Scientific Computing*. Second Edition. Cambridge University Press.

## See Also

[integrate](#), [distrExIntegrate](#)

## Examples

```
integrate(dnorm, -1.96, 1.96)
GLIntegrate(dnorm, -1.96, 1.96)
```

---

HellingerDist	<i>Generic function for the computation of the Hellinger distance of two distributions</i>
---------------	--

---

## Description

Generic function for the computation of the Hellinger distance  $d_h$  of two distributions  $P$  and  $Q$  which may be defined for an arbitrary sample space  $(\Omega, \mathcal{A})$ . The Hellinger distance is defined as

$$d_h(P, Q) = \frac{1}{2} \int |\sqrt{dP} - \sqrt{dQ}|^2$$

where  $\sqrt{dP}$ , respectively  $\sqrt{dQ}$  denotes the square root of the densities.

## Usage

```
HellingerDist(e1, e2, ...)
## S4 method for signature 'AbscontDistribution,AbscontDistribution'
HellingerDist(e1,e2,
             rel.tol=.Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"),
             IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,DiscreteDistribution'
HellingerDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,AbscontDistribution'
HellingerDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,DiscreteDistribution'
HellingerDist(e1,e2, ...)
## S4 method for signature 'numeric,DiscreteDistribution'
HellingerDist(e1, e2, ...)
## S4 method for signature 'DiscreteDistribution,numERIC'
HellingerDist(e1, e2, ...)
## S4 method for signature 'numeric,AbscontDistribution'
HellingerDist(e1, e2, asis.smooth.discretize = "discretize",
             n.discr = getdistrExOption("nDiscretize"), low.discr = getLow(e2),
             up.discr = getUp(e2), h.smooth = getdistrExOption("hSmooth"),
             rel.tol=.Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"),
             IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,numERIC'
HellingerDist(e1, e2, asis.smooth.discretize = "discretize",
             n.discr = getdistrExOption("nDiscretize"), low.discr = getLow(e1),
             up.discr = getUp(e1), h.smooth = getdistrExOption("hSmooth"),
             rel.tol=.Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"),
             IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AcDcLcDistribution,AcDcLcDistribution'
```

```
HellingerDist(e1,e2,
             rel.tol=.Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"),
             IQR.fac = 15, ..., diagnostic = FALSE)
```

## Arguments

e1	object of class "Distribution" or class "numeric"
e2	object of class "Distribution" or class "numeric"
asis.smooth.discretize	possible methods are "asis", "smooth" and "discretize". Default is "discretize".
n.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the number of lattice points used to discretize the abs. cont. distribution.
low.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the lower end point of the lattice used to discretize the abs. cont. distribution.
up.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the upper end point of the lattice used to discretize the abs. cont. distribution.
h.smooth	if asis.smooth.discretize is equal to "smooth" – i.e., the empirical distribution of the provided data should be smoothed – one has to specify this parameter.
rel.tol	relative accuracy requested in integration
TruncQuantile	Quantile the quantile based integration bounds (see details)
IQR.fac	Factor for the scale based integration bounds (see details)
...	further arguments to be used in particular methods – (in package <b>distrEx</b> : just used for distributions with a.c. parts, where it is used to pass on arguments to <b>distrExIntegrate</b> ).
diagnostic	logical; if TRUE, the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries method ("integrate" or "GLIntegrate"), call, result (the complete return value of the method), args (the args with which the method was called), and time (the time to compute the integral).

## Details

For distances between absolutely continuous distributions, we use numerical integration; to determine sensible bounds we proceed as follows: by means of `min(getLow(e1,eps=TruncQuantile),getLow(e2,eps=TruncQuantile),max(getUp(e1,eps=TruncQuantile),getUp(e2,eps=TruncQuantile))` we determine quantile based bounds  $c(\text{low.}0, \text{up.}0)$ , and by means of  $s1 <- \max(\text{IQR}(e1), \text{IQR}(e2)); m1 <- \text{median}(e1); m2 <- \text{median}(e2)$  and  $\text{low.}1 <- \min(m1, m2) - s1 * \text{IQR}.fac, \text{up.}1 <- \max(m1, m2) + s1 * \text{IQR}.fac$  we determine scale based bounds; these are combined by  $\text{low} <- \max(\text{low.}0, \text{low.}1), \text{up} <- \max(\text{up.}0, \text{up1})$ .

In case we want to compute the Hellinger distance between (empirical) data and an abs. cont. distribution, we can specify the parameter `asis.smooth.discretize` to avoid trivial distances (distance = 1).

Using `asis.smooth.discretize = "discretize"`, which is the default, leads to a discretization of the provided abs. cont. distribution and the distance is computed between the provided data and the discretized distribution.

Using `asis.smooth.discretize = "smooth"` causes smoothing of the empirical distribution of the provided data. This is, the empirical data is convoluted with the normal distribution `Norm(mean = 0, sd = h.smooth)` which leads to an abs. cont. distribution. Afterwards the distance between the smoothed empirical distribution and the provided abs. cont. distribution is computed.

Diagnostics on the involved integrations are available if argument `diagnostic` is TRUE. Then there is attribute `diagnostic` attached to the return value, which may be inspected and accessed through `showDiagnostic` and `getDiagnostic`.

### Value

Hellinger distance of e1 and e2

### Methods

- e1 = "AbscontDistribution", e2 = "AbscontDistribution":** Hellinger distance of two absolutely continuous univariate distributions which is computed using `distrExintegrate`.
- e1 = "AbscontDistribution", e2 = "DiscreteDistribution":** Hellinger distance of absolutely continuous and discrete univariate distributions (are mutually singular; i.e., have distance =1).
- e1 = "DiscreteDistribution", e2 = "DiscreteDistribution":** Hellinger distance of two discrete univariate distributions which is computed using `support` and `sum`.
- e1 = "DiscreteDistribution", e2 = "AbscontDistribution":** Hellinger distance of discrete and absolutely continuous univariate distributions (are mutually singular; i.e., have distance =1).
- e1 = "numeric", e2 = "DiscreteDistribution":** Hellinger distance between (empirical) data and a discrete distribution.
- e1 = "DiscreteDistribution", e2 = "numeric":** Hellinger distance between (empirical) data and a discrete distribution.
- e1 = "numeric", e2 = "AbscontDistribution":** Hellinger distance between (empirical) data and an abs. cont. distribution.
- e1 = "AbscontDistribution", e1 = "numeric":** Hellinger distance between (empirical) data and an abs. cont. distribution.
- e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution":** Hellinger distance of mixed discrete and absolutely continuous univariate distributions.

### Author(s)

Matthias Kohl <[Matthias.Kohl@stamats.de](mailto:Matthias.Kohl@stamats.de)>,  
Peter Ruckdeschel <[peter.ruckdeschel@uni-oldenburg.de](mailto:peter.ruckdeschel@uni-oldenburg.de)>

### References

- Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.
- Rieder, H. (1994) *Robust Asymptotic Statistics*. New York: Springer.

### See Also

[distrExIntegrate](#), [ContaminationSize](#), [TotalVarDist](#), [KolmogorovDist](#), [Distribution-class](#)

## Examples

```

HellingerDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
      mixCoeff=c(0.2,0.8)))
HellingerDist(Norm(), Td(10))
HellingerDist(Norm(mean = 50, sd = sqrt(25)), Binom(size = 100)) # mutually singular
HellingerDist(Pois(10), Binom(size = 20))

x <- rnorm(100)
HellingerDist(Norm(), x)
HellingerDist(x, Norm(), asis.smooth.discretize = "smooth")

y <- (rbinom(50, size = 20, prob = 0.5)-10)/sqrt(5)
HellingerDist(y, Norm())
HellingerDist(y, Norm(), asis.smooth.discretize = "smooth")

HellingerDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5))

```

**KolmogorovDist**

*Generic function for the computation of the Kolmogorov distance of two distributions*

## Description

Generic function for the computation of the Kolmogorov distance  $d_\kappa$  of two distributions  $P$  and  $Q$  where the distributions are defined on a finite-dimensional Euclidean space  $(\mathbf{R}^m, \mathcal{B}^m)$  with  $\mathcal{B}^m$  the Borel- $\sigma$ -algebra on  $R^m$ . The Kolmogorov distance is defined as

$$d_\kappa(P, Q) = \sup\{|P(\{y \in \mathbf{R}^m \mid y \leq x\}) - Q(\{y \in \mathbf{R}^m \mid y \leq x\})| \mid x \in \mathbf{R}^m\}$$

where  $\leq$  is coordinatewise on  $\mathbf{R}^m$ .

## Usage

```

KolmogorovDist(e1, e2, ...)
## S4 method for signature 'AbscontDistribution,AbscontDistribution'
KolmogorovDist(e1,e2, ...)
## S4 method for signature 'AbscontDistribution,DiscreteDistribution'
KolmogorovDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,AbscontDistribution'
KolmogorovDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,DiscreteDistribution'
KolmogorovDist(e1,e2, ...)
## S4 method for signature 'numeric,UnivariateDistribution'
KolmogorovDist(e1, e2, ...)
## S4 method for signature 'UnivariateDistribution,numeric'
KolmogorovDist(e1, e2, ...)
## S4 method for signature 'AcDcLcDistribution,AcDcLcDistribution'
KolmogorovDist(e1, e2, ...)

```

### Arguments

e1	object of class "Distribution" or class "numeric"
e2	object of class "Distribution" or class "numeric"
...	further arguments to be used in particular methods (not in package <b>distrEx</b> )

### Value

Kolmogorov distance of e1 and e2

### Methods

- e1 = "AbscontDistribution", e2 = "AbscontDistribution":** Kolmogorov distance of two absolutely continuous univariate distributions which is computed using a union of a (pseudo-)random and a deterministic grid.
- e1 = "DiscreteDistribution", e2 = "DiscreteDistribution":** Kolmogorov distance of two discrete univariate distributions. The distance is attained at some point of the union of the supports of e1 and e2.
- e1 = "AbscontDistribution", e2 = "DiscreteDistribution":** Kolmogorov distance of absolutely continuous and discrete univariate distributions. It is computed using a union of a (pseudo-)random and a deterministic grid in combination with the support of e2.
- e1 = "DiscreteDistribution", e2 = "AbscontDistribution":** Kolmogorov distance of discrete and absolutely continuous univariate distributions. It is computed using a union of a (pseudo-)random and a deterministic grid in combination with the support of e1.
- e1 = "numeric", e2 = "UnivariateDistribution":** Kolmogorov distance between (empirical) data and a univariate distribution. The computation is based on ks.test.
- e1 = "UnivariateDistribution", e2 = "numeric":** Kolmogorov distance between (empirical) data and a univariate distribution. The computation is based on ks.test.
- e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution":** Kolmogorov distance of mixed discrete and absolutely continuous univariate distributions. It is computed using a union of the discrete part, a (pseudo-)random and a deterministic grid in combination with the support of e1.

### Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>,  
Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

### References

- Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.  
Rieder, H. (1994) *Robust Asymptotic Statistics*. New York: Springer.

### See Also

[ContaminationSize](#), [TotalVarDist](#), [HellingerDist](#), [Distribution-class](#)

## Examples

```
KolmogorovDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
      mixCoeff=c(0.2,0.8)))
KolmogorovDist(Norm(), Td(10))
KolmogorovDist(Norm(mean = 50, sd = sqrt(25)), Binom(size = 100))
KolmogorovDist(Pois(10), Binom(size = 20))
KolmogorovDist(Norm(), rnorm(100))
KolmogorovDist(rbinom(50, size = 20, prob = 0.5)-10)/sqrt(5), Norm())
KolmogorovDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5))
```

liesInSupport

*Generic Function for Testing the Support of a Distribution*

## Description

The function tests if  $x$  lies in the support of the distribution object.

## Usage

```
## S4 method for signature 'DiscreteMVDistribution,numeric'
liesInSupport(object, x, checkFin = FALSE)
## S4 method for signature 'DiscreteMVDistribution,matrix'
liesInSupport(object, x, checkFin = FALSE)
```

## Arguments

object	object of class "Distribution"
$x$	numeric vector or matrix
checkFin	logical: in case FALSE, we simply check whether $x$ lies exactly in the <i>numerical</i> support (of finitely many support points); later on we might try to mimick the univariate case more closely in case TRUE, but so far this is not yet used.

## Value

logical vector

## Methods

**object = "DiscreteMVDistribution", x = "numeric":** does  $x$  lie in the support of object.  
**object = "DiscreteMVDistribution", x = "matrix":** does  $x$  lie in the support of object.

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## See Also

[Distribution-class](#)

## Examples

```
M <- matrix(rpois(30, lambda = 10), ncol = 3)
D1 <- DiscreteMVNDistribution(M)
M1 <- rbind(r(D1)(10), matrix(rpois(30, lam = 10), ncol = 3))
liesInSupport(D1, M1)
```

LMCondDistribution	<i>Generating function for the conditional distribution of a linear regression model.</i>
--------------------	---

## Description

Generates an object of class "AbscontCondDistribution" which is the conditional distribution of a linear regression model (given the regressor).

## Usage

```
LMCondDistribution(Error = Norm(), theta = 0, intercept = 0, scale = 1)
```

## Arguments

- |           |  |
|-----------|--|
| Error     | Object of class "AbscontDistribution": error distribution. |
| theta     | numeric vector: regression parameter.                      |
| intercept | real number: intercept parameter.                          |
| scale     | positive real number: scale parameter.                     |

## Value

Object of class "AbscontCondDistribution"

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## See Also

[AbscontCondDistribution-class](#), [E-methods](#)

## Examples

```
# normal error distribution
(D1 <- LMCondDistribution(theta = 1)) # corresponds to Norm(cond, 1)
plot(D1)
r(D1)
d(D1)
p(D1)
q(D1)
## in RStudio or Jupyter IRKernel, use q.l(.)(.) instead of q(.)(.)
```

```

param(D1)
cond(D1)

d(D1)(θ, cond = 1)
d(Norm(mean=1))(θ)

E(D1, cond = 1)
E(D1, function(x){x^2}, cond = 2)
E(Norm(mean=2), function(x){x^2})

```

**LMParameter***Generating function for LMParameter-class***Description**

Generates an object of class "LMParameter".

**Usage**

```
LMParameter(theta = 0, intercept = 0, scale = 1)
```

**Arguments**

theta	numeric vector: regression parameter (default =0).
intercept	real number: intercept parameter (default =0).
scale	positive real number: scale parameter (default =1).

**Value**

Object of class "LMParameter"

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[LMParameter-class](#)

**Examples**

```

LMParameter(theta = c(1,1), intercept = 2, scale = 0.5)

## The function is currently defined as
function(theta = 0, intercept = 0, scale = 1){
  new("LMParameter", theta = theta, intercept = intercept, scale = 1)
}

```

**LMPParameter-class**      *Parameter of a linear regression model*

## Description

Parameter of a linear regression model

$$y = \mu + x^\tau \theta + \sigma u$$

with intercept  $\mu$ , regression parameter  $\theta$  and error scale  $\sigma$ .

## Objects from the Class

Objects can be created by calls of the form `new("LMPParameter", ...)`. More frequently they are created via the generating function `LMPParameter`.

## Slots

`theta` numeric vector: regression parameter.  
`intercept` real number: intercept parameter.  
`scale` positive real number: scale parameter.  
`name` character vector: the default name is “parameter of a linear regression model”.

## Extends

Class “Parameter”, directly.  
Class “OptionalParameter”, by class “Parameter”.

## Methods

`show` `signature(object = "LMPParameter")`

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## See Also

[Parameter-class](#), [LMPParameter](#)

## Examples

```
new("LMPParameter")
```

---

m1df*Generic Function for the Computation of Clipped First Moments*

---

## Description

Generic function for the computation of clipped first moments. The moments are clipped at upper.

## Usage

```
m1df(object, upper, ...)
## S4 method for signature 'AbscontDistribution'
m1df(object, upper,
      lowerTruncQuantile = getdistrExOption("m1dfLowerTruncQuantile"),
      rel.tol = getdistrExOption("m1dfRelativeTolerance"), ...)
```

## Arguments

object	object of class "Distribution"
upper	clipping bound
rel.tol	relative tolerance for distrExIntegrate.
lowerTruncQuantile	lower quantile for quantile based integration range.
...	additional arguments to E

## Details

The precision of the computations can be controlled via certain global options; cf. [distrExOptions](#).

## Value

The first moment of object clipped at upper is computed.

## Methods

**object = "UnivariateDistribution":** uses call E(object, upp=upper, ...).

**object = "AbscontDistribution":** clipped first moment for absolutely continuous univariate distributions which is computed using integrate.

**object = "LatticeDistribution":** clipped first moment for discrete univariate distributions which is computed using support and sum.

**object = "AffLinDistribution":** clipped first moment for affine linear distributions which is computed on basis of slot X0.

**object = "Binom":** clipped first moment for Binomial distributions which is computed using pbiniom.

**object = "Pois":** clipped first moment for Poisson distributions which is computed using ppois.

**object = "Norm":** clipped first moment for normal distributions which is computed using dnorm and pnorm.

**object = "Exp":** clipped first moment for exponential distributions which is computed using pexp.

**object = "Chisq":** clipped first moment for  $\chi^2$  distributions which is computed using pchisq.

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[distrExIntegrate](#), [m2df](#), [E](#)

**Examples**

```
# standard normal distribution
N1 <- Norm()
m1df(N1, 0)

# Poisson distribution
P1 <- Pois(lambda=2)
m1df(P1, 3)
m1df(P1, 3, fun = function(x)sin(x))

# absolutely continuous distribution
D1 <- Norm() + Exp() # convolution
m1df(D1, 2)
m1df(D1, Inf)
E(D1)
```

**m2df**

*Generic function for the computation of clipped second moments*

**Description**

Generic function for the computation of clipped second moments. The moments are clipped at upper.

**Usage**

```
m2df(object, upper, ...)
## S4 method for signature 'AbscontDistribution'
m2df(object, upper,
      lowerTruncQuantile = getdistrExOption("m2dfLowerTruncQuantile"),
      rel.tol = getdistrExOption("m2dfRelativeTolerance"), ...)
```

**Arguments**

object	object of class "Distribution"
upper	clipping bound
rel.tol	relative tolerance for <a href="#">distrExIntegrate</a> .
lowerTruncQuantile	lower quantile for quantile based integration range.
...	additional arguments to E

## Details

The precision of the computations can be controlled via certain global options; cf. [distrExOptions](#).

## Value

The second moment of object clipped at upper is computed.

## Methods

- object = "UnivariateDistribution"**: uses call E(object, upp=upper, fun = function, ...).
- object = "AbscontDistribution"**: clipped second moment for absolutely continuous univariate distributions which is computed using integrate.
- object = "LatticeDistribution"**: clipped second moment for discrete univariate distributions which is computed using support and sum.
- object = "AffLinDistribution"**: clipped second moment for affine linear distributions which is computed on basis of slot X0.
- object = "Binom"**: clipped second moment for Binomial distributions which is computed using pbinom.
- object = "Pois"**: clipped second moment for Poisson distributions which is computed using ppois.
- object = "Norm"**: clipped second moment for normal distributions which is computed using dnorm and pnorm.
- object = "Exp"**: clipped second moment for exponential distributions which is computed using pexp.
- object = "Chisq"**: clipped second moment for  $\chi^2$  distributions which is computed using pchisq.

## Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

## See Also

[m2df-methods](#), [E-methods](#)

## Examples

```
# standard normal distribution
N1 <- Norm()
m2df(N1, 0)

# Poisson distribution
P1 <- Pois(lambda=2)
m2df(P1, 3)
m2df(P1, 3, fun = function(x)sin(x))

# absolutely continuous distribution
D1 <- Norm() + Exp() # convolution
m2df(D1, 2)
m2df(D1, Inf)
E(D1, function(x){x^2})
```

## Description

The function `make01` produces a new centered and standardized univariate distribution.

## Usage

```
make01(x)
```

## Arguments

<code>x</code>	an object of class "UnivariateDistribution"
----------------	---

## Details

Thanks to the functionals provided in this package, the code is a one-liner:  $(x - E(x)) / sd(x)$ .

## Value

Object of class "UnivariateDistribution" with expectation 0 and variance 1.

## Author(s)

Peter Ruckdeschel <[peter.ruckdeschel@uni-oldenburg.de](mailto:peter.ruckdeschel@uni-oldenburg.de)>

## See Also

`E`, `Var`

## Examples

```
X <- sin(exp(2*log(abs( Norm())))) ## something weird
X01 <- make01(X)
print(X01)
plot(X01)
sd(X01); E(X01)
```

---

**MultivariateDistribution-class**  
*Multivariate Distributions*

---

**Description**

The class of multivariate distributions. One has at least to specify the image space of the distribution and a function generating (pseudo-)random numbers. The slot `q` is usually filled with `NULL` for dimensions > 1.

**Objects from the Class**

Objects can be created by calls of the form `new("MultivariateDistribution", ...)`.

**Slots**

- `img` Object of class "rSpace". Image space of the distribution. Usually an object of class "EuclideanSpace".
- `param` Object of class "OptionalParameter". Optional parameter of the multivariate distribution.
- `r` Object of class "function": generates (pseudo-)random numbers
- `d` Object of class "OptionalFunction": optional density function
- `p` Object of class "OptionalFunction": optional cumulative distribution function
- `q` Object of class "OptionalFunction": optional quantile function
- `.withArith` logical: used internally to issue warnings as to interpretation of arithmetics
- `.withSim` logical: used internally to issue warnings as to accuracy
- `.logExact` logical: used internally to flag the case where there are explicit formulae for the log version of density, cdf, and quantile function
- `.lowerExact` logical: used internally to flag the case where there are explicit formulae for the lower tail version of cdf and quantile function
- `Symmetry` object of class "DistributionSymmetry"; used internally to avoid unnecessary calculations.

**Extends**

Class "Distribution", directly.

**Methods**

- `show` signature(`object = "MultivariateDistribution"`)
- `plot` signature(`object = "MultivariateDistribution"`): not yet implemented.

**Author(s)**

Matthias Kohl <[Matthias.Kohl@stamats.de](mailto:Matthias.Kohl@stamats.de)>

**See Also**

[Distribution-class](#)

**Examples**

```
# Dirac-measure in (0,0)
new("MultivariateDistribution")
```

OAsymTotalVarDist

*Generic function for the computation of (minimal) asymmetric total variation distance of two distributions*

**Description**

Generic function for the computation of (minimal) asymmetric total variation distance  $d_v^*$  of two distributions  $P$  and  $Q$  where the distributions may be defined for an arbitrary sample space  $(\Omega, \mathcal{A})$ . This distance is defined as

$$d_v^*(P, Q) = \min_c \int |dQ - c dP|$$

**Usage**

```
OAsymTotalVarDist(e1, e2, ...)
## S4 method for signature 'AbscontDistribution,AbscontDistribution'
OAsymTotalVarDist(e1,e2,
                  rel.tol = .Machine$double.eps^0.3, Ngrid = 10000,
                  TruncQuantile = getdistrOption("TruncQuantile"),
                  IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,DiscreteDistribution'
OAsymTotalVarDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,AbscontDistribution'
OAsymTotalVarDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,DiscreteDistribution'
OAsymTotalVarDist(e1,e2, ...)
## S4 method for signature 'numeric,DiscreteDistribution'
OAsymTotalVarDist(e1, e2, ...)
## S4 method for signature 'DiscreteDistribution,numeric'
OAsymTotalVarDist(e1, e2, ...)
## S4 method for signature 'numeric,AbscontDistribution'
OAsymTotalVarDist(e1, e2, asis.smooth.discretize = "discretize",
                  n.dscr = getdistrExOption("nDiscretize"), low.dscr = getLow(e2),
                  up.dscr = getUp(e2), h.smooth = getdistrExOption("hSmooth"),
                  rel.tol = .Machine$double.eps^0.3, Ngrid = 10000,
                  TruncQuantile = getdistrOption("TruncQuantile"),
                  IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,numeric'
OAsymTotalVarDist(e1, e2,
```

```

asis.smooth.discretize = "discretize",
n.discr = getdistrExOption("nDiscretize"), low.discr = getLow(e1),
up.discr = getUp(e1), h.smooth = getdistrExOption("hSmooth"),
rel.tol = .Machine$double.eps^0.3, Ngrid = 10000,
TruncQuantile = getdistrOption("TruncQuantile"),
IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AcDcLcDistribution,AcDcLcDistribution'
OAsymTotalVarDist(e1, e2,
                   rel.tol = .Machine$double.eps^0.3, Ngrid = 10000,
                   TruncQuantile = getdistrOption("TruncQuantile"),
                   IQR.fac = 15, ..., diagnostic = FALSE)

```

## Arguments

e1	object of class "Distribution" or "numeric"
e2	object of class "Distribution" or "numeric"
asis.smooth.discretize	possible methods are "asis", "smooth" and "discretize". Default is "discretize".
n.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the number of lattice points used to discretize the abs. cont. distribution.
low.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the lower end point of the lattice used to discretize the abs. cont. distribution.
up.discr	if asis.smooth.discretize is equal to "discretize" one has to specify the upper end point of the lattice used to discretize the abs. cont. distribution.
h.smooth	if asis.smooth.discretize is equal to "smooth" – i.e., the empirical distribution of the provided data should be smoothed – one has to specify this parameter.
rel.tol	relative tolerance for distrExIntegrate and uniroot
Ngrid	How many grid points are to be evaluated to determine the range of the likelihood ratio?
,	
TruncQuantile	Quantile the quantile based integration bounds (see details)
IQR.fac	Factor for the scale based integration bounds (see details)
...	further arguments to be used in particular methods – (in package <b>distrEx</b> : just used for distributions with a.c. parts, where it is used to pass on arguments to <b>distrExIntegrate</b> ).
diagnostic	logical; if TRUE, the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries method ("integrate" or "GLIntegrate"), call, result (the complete return value of the method), args (the args with which the method was called), and time (the time to compute the integral).

## Details

For distances between absolutely continuous distributions, we use numerical integration; to determine sensible bounds we proceed as follows: by means of `min(getLow(e1, eps=TruncQuantile),getLow(e2,eps=TruncQ`

`max(getUp(e1,eps=TruncQuantile),getUp(e2,eps=TruncQuantile))` we determine quantile based bounds  $c(\text{low.0}, \text{up.0})$ , and by means of  $s1 <- \max(\text{IQR}(e1), \text{IQR}(e2))$ ;  $m1 <- \text{median}(e1)$ ;  $m2 <- \text{median}(e2)$  and  $\text{low.1} <- \min(m1, m2) - s1 * \text{IQR}.fac$ ,  $\text{up.1} <- \max(m1, m2) + s1 * \text{IQR}.fac$  we determine scale based bounds; these are combined by  $\text{low} <- \max(\text{low.0}, \text{low.1})$ ,  $\text{up} <- \max(\text{up.0}, \text{up.1})$ .

Again in the absolutely continuous case, to determine the range of the likelihood ratio, we evaluate this ratio on a grid constructed as follows:  $x.\text{range} <- c(\text{seq}(\text{low}, \text{up}, \text{length}=Ngrid/3), q.l(e1)(\text{seq}(0, 1, \text{length}=Ngrid/3) * .999), q.l(e2)(\text{seq}(0, 1, \text{length}=Ngrid/3) * .999))$

Finally, for both discrete and absolutely continuous case, we clip this ratio downwards by  $1e-10$  and upwards by  $1e10$

In case we want to compute the total variation distance between (empirical) data and an abs. cont. distribution, we can specify the parameter `asis.smooth.discretize` to avoid trivial distances (distance = 1).

Using `asis.smooth.discretize = "discretize"`, which is the default, leads to a discretization of the provided abs. cont. distribution and the distance is computed between the provided data and the discretized distribution.

Using `asis.smooth.discretize = "smooth"` causes smoothing of the empirical distribution of the provided data. This is, the empirical data is convoluted with the normal distribution `Norm(mean = 0, sd = h.smooth)` which leads to an abs. cont. distribution. Afterwards the distance between the smoothed empirical distribution and the provided abs. cont. distribution is computed.

Diagnostics on the involved integrations are available if argument `diagnostic` is TRUE. Then there is attribute `diagnostic` attached to the return value, which may be inspected and accessed through `showDiagnostic` and `getDiagnostic`.

## Value

OAsymmetric Total variation distance of e1 and e2

## Methods

**e1 = "AbscontDistribution", e2 = "AbscontDistribution":** total variation distance of two absolutely continuous univariate distributions which is computed using `distrExIntegrate`.

**e1 = "AbscontDistribution", e2 = "DiscreteDistribution":** total variation distance of absolutely continuous and discrete univariate distributions (are mutually singular; i.e., have distance =1).

**e1 = "DiscreteDistribution", e2 = "DiscreteDistribution":** total variation distance of two discrete univariate distributions which is computed using `support` and `sum`.

**e1 = "DiscreteDistribution", e2 = "AbscontDistribution":** total variation distance of discrete and absolutely continuous univariate distributions (are mutually singular; i.e., have distance =1).

**e1 = "numeric", e2 = "DiscreteDistribution":** Total variation distance between (empirical) data and a discrete distribution.

**e1 = "DiscreteDistribution", e2 = "numeric":** Total variation distance between (empirical) data and a discrete distribution.

**e1 = "numeric", e2 = "AbscontDistribution":** Total variation distance between (empirical) data and an abs. cont. distribution.

**e1 = "AbscontDistribution", e1 = "numeric":** Total variation distance between (empirical) data and an abs. cont. distribution.

**e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution":** Total variation distance of mixed discrete and absolutely continuous univariate distributions.

### Author(s)

Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

### References

to be filled; Agostinelli, C and Ruckdeschel, P. (2009): A simultaneous inlier and outlier model by asymmetric total variation distance.

### See Also

[TotalVarDist-methods](#), [ContaminationSize](#), [KolmogorovDist](#), [HellingerDist](#), [Distribution-class](#)

### Examples

```
OAsymTotalVarDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
          mixCoeff=c(0.2,0.8)))
OAsymTotalVarDist(Norm(), Td(10))
OAsymTotalVarDist(Norm(mean = 50, sd = sqrt(25)), Binom(size = 100)) # mutually singular
OAsymTotalVarDist(Pois(10), Binom(size = 20))

x <- rnorm(100)
OAsymTotalVarDist(Norm(), x)
OAsymTotalVarDist(x, Norm(), asis.smooth.discretize = "smooth")

y <- (rbinom(50, size = 20, prob = 0.5)-10)/sqrt(5)
OAsymTotalVarDist(y, Norm())
OAsymTotalVarDist(y, Norm(), asis.smooth.discretize = "smooth")

OAsymTotalVarDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5))
```

### Description

plot-methods

### Usage

```
plot(x, y, ...)
## S4 method for signature 'UnivariateCondDistribution,missing'
plot(x, y, ...)
## S4 method for signature 'MultivariateDistribution,missing'
plot(x, y, ...)
```

### Arguments

- x object of class "UnivariateCondDistribution" or class "MultivariateDistribution": distribution(s) which should be plotted
- y missing
- ... additional arguments

### Details

upto now only warnings are issued that the corresponding method is not yet implemented;

**PrognCondDistribution** *Generating function for PrognCondDistribution-class*

### Description

Generates an object of class "PrognCondDistribution".

### Usage

```
PrognCondDistribution(Regr, Error,
                      rel.tol= getdistrExOption("ErelativeTolerance"),
                      lowerTruncQuantile = getdistrExOption("ElowerTruncQuantile"),
                      upperTruncQuantile = getdistrExOption("EupperTruncQuantile"),
                      IQR.fac = getdistrExOption("IQR.fac"))
```

### Arguments

- Regr object of class AbscontDistribution; the distribution of X.
- Error object of class AbscontDistribution; the distribution of eps.
- rel.tol relative tolerance for distrExIntegrate.
- lowerTruncQuantile lower quantile for quantile based integration range.
- upperTruncQuantile upper quantile for quantile based integration range.
- IQR.fac factor for scale based integration range (i.e.; median of the distribution  $\pm$  IQR.fac  $\times$  IQR).

### Details

For independent r.v.'s X,E with univariate, absolutely continuous (a.c.) distributions Regr and Error, respectively, PrognCondDistribution() returns the (factorized, conditional) posterior distribution of X given X+E=y. as an object of class PrognCondDistribution.

### Value

Object of class "PrognCondDistribution"

**Author(s)**

Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>,

**See Also**

PrognCondDistribution-class; demo('Prognose.R').

**Examples**

```
PrognCondDistribution(Error = ConvexContamination(Norm(), Norm(4,1), size=0.1))
```

**PrognCondDistribution-class**

*Posterior distribution in convolution*

**Description**

The posterior distribution of X given (X+E)=y

**Objects from the Class**

Objects can be created by calls of the form [PrognCondDistribution](#) where `Regr` and `error` are the respective (a.c.) distributions of X and E and the other arguments control accuracy in integration.

**Slots**

- cond:** Object of class "PrognCondition": condition
- img:** Object of class "rSpace": the image space.
- param:** Object of class "OptionalParameter": an optional parameter.
- r:** Object of class "function": generates random numbers.
- d:** Object of class "OptionalFunction": optional conditional density function.
- p:** Object of class "OptionalFunction": optional conditional cumulative distribution function.
- q:** Object of class "OptionalFunction": optional conditional quantile function.
- gaps:** (numeric) matrix or NULL
- .withArith:** logical: used internally to issue warnings as to interpretation of arithmetics
- .withSim:** logical: used internally to issue warnings as to accuracy
- .logExact:** logical: used internally to flag the case where there are explicit formulae for the log version of density, cdf, and quantile function
- .lowerExact:** logical: used internally to flag the case where there are explicit formulae for the lower tail version of cdf and quantile function

**Extends**

Class "AbscontCondDistribution", directly.

Class "Distribution", by classes "UnivariateCondDistribution" and "AbscontCondDistribution".

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[PrognCondition-class](#), [UnivariateCondDistribution-class](#) [AbscontCondDistribution-class](#),  
[Distribution-class](#)

**Examples**

```
PrognCondDistribution()
```

*PrognCondition-class    Conditions of class 'PrognCondition'*

**Description**

The class PrognCondition realizes the condition that  $X+E=y$  in a convolution setup

**Usage**

```
PrognCondition(range = EuclideanSpace())
```

**Arguments**

range	an object of class "EuclideanSpace"
-------	-------------------------------------

**Value**

Object of class "PrognCondition"

**Objects from the Class**

Objects can be created by calls of the form `PrognCondition(range)`.

**Slots**

name Object of class "character": name of the PrognCondition

range Object of class "EuclideanSpace": range of the PrognCondition

**Extends**

Class "Condition", directly.

**Methods**

```
show signature(object = "PrognCondition")
```

**Author(s)**

Matthias Kohl <Matthias.Kohl@stamats.de>

**See Also**

[PrognCondDistribution-class](#), [Condition-class](#)

**Examples**

`PrognCondition()`

`TotalVarDist`

*Generic function for the computation of the total variation distance of two distributions*

**Description**

Generic function for the computation of the total variation distance  $d_v$  of two distributions  $P$  and  $Q$  where the distributions may be defined for an arbitrary sample space  $(\Omega, \mathcal{A})$ . The total variation distance is defined as

$$d_v(P, Q) = \sup_{B \in \mathcal{A}} |P(B) - Q(B)|$$

**Usage**

```
TotalVarDist(e1, e2, ...)
## S4 method for signature 'AbscontDistribution,AbscontDistribution'
TotalVarDist(e1,e2,
             rel.tol=.Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"),
             IQR.fac = 15, ..., diagnostic = FALSE)
## S4 method for signature 'AbscontDistribution,DiscreteDistribution'
TotalVarDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,AbscontDistribution'
TotalVarDist(e1,e2, ...)
## S4 method for signature 'DiscreteDistribution,DiscreteDistribution'
TotalVarDist(e1,e2, ...)
## S4 method for signature 'numeric,DiscreteDistribution'
TotalVarDist(e1, e2, ...)
## S4 method for signature 'DiscreteDistribution,numERIC'
TotalVarDist(e1, e2, ...)
## S4 method for signature 'numeric,AbscontDistribution'
TotalVarDist(e1, e2, asis.smooth.discretize = "discretize",
             n.dscr = getdistrExOption("nDiscretize"), low.dscr = getLow(e2),
             up.dscr = getUp(e2), h.smooth = getdistrExOption("hSmooth"),
             rel.tol = .Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"), IQR.fac = 15, ...,
             diagnostic = FALSE)
```

```

## S4 method for signature 'AbscontDistribution,numeric'
TotalVarDist(e1, e2, asis.smooth.discretize = "discretize",
             n.dscr = getdistrExOption("nDiscretize"), low.dscr = getLow(e1),
             up.dscr = getUp(e1), h.smooth = getdistrExOption("hSmooth"),
             rel.tol = .Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"), IQR.fac = 15, ...,
             diagnostic = FALSE)
## S4 method for signature 'AcDcLcDistribution,AcDcLcDistribution'
TotalVarDist(e1, e2,
             rel.tol = .Machine$double.eps^0.3,
             TruncQuantile = getdistrOption("TruncQuantile"),
             IQR.fac = 15, ..., diagnostic = FALSE)

```

## Arguments

e1	object of class "Distribution" or "numeric"
e2	object of class "Distribution" or "numeric"
asis.smooth.discretize	possible methods are "asis", "smooth" and "discretize". Default is "discretize".
n.dscr	if asis.smooth.discretize is equal to "discretize" one has to specify the number of lattice points used to discretize the abs. cont. distribution.
low.dscr	if asis.smooth.discretize is equal to "discretize" one has to specify the lower end point of the lattice used to discretize the abs. cont. distribution.
up.dscr	if asis.smooth.discretize is equal to "discretize" one has to specify the upper end point of the lattice used to discretize the abs. cont. distribution.
h.smooth	if asis.smooth.discretize is equal to "smooth" – i.e., the empirical distribution of the provided data should be smoothed – one has to specify this parameter.
rel.tol	relative accuracy requested in integration
TruncQuantile	Quantile the quantile based integration bounds (see details)
IQR.fac	Factor for the scale based integration bounds (see details)
...	further arguments to be used in particular methods – (in package <b>distrEx</b> : just used for distributions with a.c. parts, where it is used to pass on arguments to <b>distrExIntegrate</b> ).
diagnostic	logical; if TRUE, the return value obtains an attribute "diagnostic" with diagnostic information on the integration, i.e., a list with entries <b>method</b> ("integrate" or "GLIntegrate"), <b>call</b> , <b>result</b> (the complete return value of the method), <b>args</b> (the args with which the method was called), and <b>time</b> (the time to compute the integral).

## Details

For distances between absolutely continuous distributions, we use numerical integration; to determine sensible bounds we proceed as follows: by means of `min(getLow(e1, eps=TruncQuantile), getLow(e2, eps=TruncQuantile))` and `max(getUp(e1, eps=TruncQuantile), getUp(e2, eps=TruncQuantile))` we determine quantile based bounds `c(low.0, up.0)`, and by means of `s1 <- max(IQR(e1), IQR(e2)); m1 <- median(e1);`

`m2 <- median(e2) and low.1 <- min(m1,m2)-s1*IQR.fac, up.1 <- max(m1,m2)+s1*IQR.fac we determine scale based bounds; these are combined by low <- max(low.0,low.1), up <- max(up.0,up1).`

In case we want to compute the total variation distance between (empirical) data and an abs. cont. distribution, we can specify the parameter `asis.smooth.discretize` to avoid trivial distances (distance = 1).

Using `asis.smooth.discretize = "discretize"`, which is the default, leads to a discretization of the provided abs. cont. distribution and the distance is computed between the provided data and the discretized distribution.

Using `asis.smooth.discretize = "smooth"` causes smoothing of the empirical distribution of the provided data. This is, the empirical data is convoluted with the normal distribution `Norm(mean = 0, sd = h.smooth)` which leads to an abs. cont. distribution. Afterwards the distance between the smoothed empirical distribution and the provided abs. cont. distribution is computed.

Diagnostics on the involved integrations are available if argument `diagnostic` is TRUE. Then there is attribute `diagnostic` attached to the return value, which may be inspected and accessed through `showDiagnostic` and `getDiagnostic`.

## Value

Total variation distance of e1 and e2

## Methods

**e1 = "AbscontDistribution", e2 = "AbscontDistribution":** total variation distance of two absolutely continuous univariate distributions which is computed using `distrExIntegrate`.

**e1 = "AbscontDistribution", e2 = "DiscreteDistribution":** total variation distance of absolutely continuous and discrete univariate distributions (are mutually singular; i.e., have distance =1).

**e1 = "DiscreteDistribution", e2 = "DiscreteDistribution":** total variation distance of two discrete univariate distributions which is computed using `support` and `sum`.

**e1 = "DiscreteDistribution", e2 = "AbscontDistribution":** total variation distance of discrete and absolutely continuous univariate distributions (are mutually singular; i.e., have distance =1).

**e1 = "numeric", e2 = "DiscreteDistribution":** Total variation distance between (empirical) data and a discrete distribution.

**e1 = "DiscreteDistribution", e2 = "numeric":** Total variation distance between (empirical) data and a discrete distribution.

**e1 = "numeric", e2 = "AbscontDistribution":** Total variation distance between (empirical) data and an abs. cont. distribution.

**e1 = "AbscontDistribution", e1 = "numeric":** Total variation distance between (empirical) data and an abs. cont. distribution.

**e1 = "AcDcLcDistribution", e2 = "AcDcLcDistribution":** Total variation distance of mixed discrete and absolutely continuous univariate distributions.

## Author(s)

Matthias Kohl <[Matthias.Kohl@stamats.de](mailto:Matthias.Kohl@stamats.de)>,  
Peter Ruckdeschel <[peter.ruckdeschel@uni-oldenburg.de](mailto:peter.ruckdeschel@uni-oldenburg.de)>

## References

- Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.  
 Rieder, H. (1994) *Robust Asymptotic Statistics*. New York: Springer.

## See Also

[TotalVarDist-methods](#), [ContaminationSize](#), [KolmogorovDist](#), [HellingerDist](#), [Distribution-class](#)

## Examples

```
TotalVarDist(Norm(), UnivarMixingDistribution(Norm(1,2),Norm(0.5,3),
                                              mixCoeff=c(0.2,0.8)))
TotalVarDist(Norm(), Td(10))
TotalVarDist(Norm(mean = 50, sd = sqrt(25)), Binom(size = 100)) # mutually singular
TotalVarDist(Pois(10), Binom(size = 20))

x <- rnorm(100)
TotalVarDist(Norm(), x)
TotalVarDist(x, Norm(), asis.smooth.discretize = "smooth")

y <- (rbinom(50, size = 20, prob = 0.5)-10)/sqrt(5)
TotalVarDist(y, Norm())
TotalVarDist(y, Norm(), asis.smooth.discretize = "smooth")

TotalVarDist(rbinom(50, size = 20, prob = 0.5), Binom(size = 20, prob = 0.5))
```

## UnivariateCondDistribution-class

*Univariate conditional distribution*

## Description

Class of univariate conditional distributions.

## Objects from the Class

Objects can be created by calls of the form `new("UnivariateCondDistribution", ...)`.

## Slots

- cond Object of class "Condition": condition
- img Object of class "rSpace": the image space.
- param Object of class "OptionalParameter": an optional parameter.
- r Object of class "function": generates random numbers.
- d Object of class "OptionalFunction": optional conditional density function.
- p Object of class "OptionalFunction": optional conditional cumulative distribution function.

q Object of class "OptionalFunction": optional conditional quantile function.  
.withArith logical: used internally to issue warnings as to interpretation of arithmetics  
.withSim logical: used internally to issue warnings as to accuracy  
.logExact logical: used internally to flag the case where there are explicit formulae for the log version of density, cdf, and quantile function  
.lowerExact logical: used internally to flag the case where there are explicit formulae for the lower tail version of cdf and quantile function  
Symmetry object of class "DistributionSymmetry"; used internally to avoid unnecessary calculations.

### Extends

Class "UnivariateDistribution", directly.  
Class "Distribution", by class "UnivariateDistribution".

### Methods

**cond** signature(object = "UnivariateCondDistribution"): accessor function for slot cond.  
**show** signature(object = "UnivariateCondDistribution")  
**plot** signature(object = "UnivariateCondDistribution"): not yet implemented.

### Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

### See Also

[Distribution-class](#)

### Examples

```
new("UnivariateCondDistribution")
```

---

### Description

Generic functions for the computation of functionals on distributions.

**Usage**

```
IQR(x, ...)

## S4 method for signature 'UnivariateDistribution'
IQR(x)
## S4 method for signature 'UnivariateCondDistribution'
IQR(x,cond)
## S4 method for signature 'AffLinDistribution'
IQR(x)
## S4 method for signature 'DiscreteDistribution'
IQR(x)
## S4 method for signature 'Arcsine'
IQR(x)
## S4 method for signature 'Cauchy'
IQR(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Dirac'
IQR(x)
## S4 method for signature 'DExp'
IQR(x)
## S4 method for signature 'Exp'
IQR(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Geom'
IQR(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Logis'
IQR(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Norm'
IQR(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Unif'
IQR(x, propagate.names=getdistrExOption("propagate.names.functionals"))

median(x, ...)

## S4 method for signature 'UnivariateDistribution'
median(x)
## S4 method for signature 'UnivariateCondDistribution'
median(x,cond)
## S4 method for signature 'AffLinDistribution'
median(x)
## S4 method for signature 'Arcsine'
median(x)
## S4 method for signature 'Cauchy'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Dirac'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'DExp'
median(x)
## S4 method for signature 'Exp'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
```

```
## S4 method for signature 'Geom'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Logis'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Lnorm'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Norm'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Unif'
median(x, propagate.names=getdistrExOption("propagate.names.functionals"))

mad(x, ...)

## S4 method for signature 'UnivariateDistribution'
mad(x)
## S4 method for signature 'AffLinDistribution'
mad(x)
## S4 method for signature 'Cauchy'
mad(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Dirac'
mad(x)
## S4 method for signature 'DExp'
mad(x)
## S4 method for signature 'Exp'
mad(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Geom'
mad(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Logis'
mad(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Norm'
mad(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Unif'
mad(x, propagate.names=getdistrExOption("propagate.names.functionals"))
## S4 method for signature 'Arcsine'
mad(x)

sd(x, ...)

## S4 method for signature 'UnivariateDistribution'
sd(x, fun, cond, withCond, useApply,
    propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Norm'
sd(x, fun, cond, withCond = FALSE, useApply = TRUE,
    propagate.names=getdistrExOption("propagate.names.functionals"), ...)

var(x, ...)

## S4 method for signature 'UnivariateDistribution'
```

```

var(x, fun, cond, withCond, useApply, ...)
## S4 method for signature 'AffLinDistribution'
var(x, fun, cond, withCond, useApply, ...)
## S4 method for signature 'CompoundDistribution'
var(x, ...)
## S4 method for signature 'Arcsine'
var(x, ...)
## S4 method for signature 'Binom'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Beta'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"),...)
## S4 method for signature 'Cauchy'
var(x, ...)
## S4 method for signature 'Chisq'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Dirac'
var(x, ...)
## S4 method for signature 'DExp'
var(x, ...)
## S4 method for signature 'Exp'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Fd'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Gammad'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Geom'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Hyper'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Logis'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Lnorm'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Nbinom'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Norm'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Pois'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Td'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Unif'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Weibull'
var(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)

skewness(x, ...)
## S4 method for signature 'UnivariateDistribution'

```

```
skewness(x, fun, cond, withCond, useApply, ...)
## S4 method for signature 'AffLinDistribution'
skewness(x, fun, cond, withCond, useApply, ...)
## S4 method for signature 'Arcsine'
skewness(x, ...)
## S4 method for signature 'Binom'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Beta'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Cauchy'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Chisq'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Dirac'
skewness(x, ...)
## S4 method for signature 'DExp'
skewness(x, ...)
## S4 method for signature 'Exp'
skewness(x, ...)
## S4 method for signature 'Fd'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Gammad'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Geom'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Hyper'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Logis'
skewness(x, ...)
## S4 method for signature 'Lnorm'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Nbinom'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Norm'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Pois'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Td'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Unif'
skewness(x, ...)
## S4 method for signature 'Weibull'
skewness(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)

kurtosis(x, ...)
## S4 method for signature 'UnivariateDistribution'
kurtosis(x, fun, cond, withCond, useApply, ...)
## S4 method for signature 'AffLinDistribution'
```

```

kurtosis(x, fun, cond, withCond, useApply, ...)
## S4 method for signature 'Arcsine'
kurtosis(x, ...)
## S4 method for signature 'Binom'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Beta'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Cauchy'
kurtosis(x, ...)
## S4 method for signature 'Chisq'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Dirac'
kurtosis(x, ...)
## S4 method for signature 'DExp'
kurtosis(x, ...)
## S4 method for signature 'Exp'
kurtosis(x, ...)
## S4 method for signature 'Fd'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Gammad'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Geom'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Hyper'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Logis'
kurtosis(x, ...)
## S4 method for signature 'Lnorm'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)
## S4 method for signature 'Nbinom'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"),...)
## S4 method for signature 'Norm'
kurtosis(x, ...)
## S4 method for signature 'Pois'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"),...)
## S4 method for signature 'Td'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"),...)
## S4 method for signature 'Unif'
kurtosis(x, ...)
## S4 method for signature 'Weibull'
kurtosis(x, propagate.names=getdistrExOption("propagate.names.functionals"), ...)

```

## Arguments

x	object of class "UnivariateDistribution"
fun	if missing the (conditional) variance resp. standard deviation is computed else the (conditional) variance resp. standard deviation of fun is computed.

cond	if not missing the conditional variance resp. standard deviation given cond is computed.
...	additional arguments to fun or E
useApply	logical: should sapply, respectively apply be used to evaluate fund.
withCond	logical: is cond in the argument list of fun.
propagate.names	logical: should names obtained from parameter coordinates be propagated to return values of specific S4 methods for functionals; defaults to the value of the respective <code>distrExption propagate.names.functionals</code> .

### Value

The value of the corresponding functional at the distribution in the argument is computed.

### Methods

<code>var, signature(x = "Any")</code> :	interface to the <b>stats</b> -function <code>var</code> — see <a href="#">var</a> resp. <code>help(var, package="stats")</code> .
<code>var, signature(x = "UnivariateDistribution")</code> :	variance of univariate distributions using corresponding <code>E()</code> -method.
<code>var, signature(x = "AffLinDistribution")</code> :	if arguments <code>fun, cond</code> are missing: $x@a^2 * var(x@X0)$ else uses method for <code>signature(x = "UnivariateDistribution")</code>
<code>var, signature(x = "CompoundDistribution")</code> :	if we are in i.i.d. situation (i.e., slot <code>SummandsDistr</code> is of class <code>UnivariateDistribution</code> ) the formula $E[N]var[S] + (E[S]^2 + var(S))var(N)$ for $N$ the frequency distribution and $S$ the summand distribution; else we coerce to " <code>UnivarLebDecDistribution</code> ".
<code>sd, signature(x = "Any")</code> :	interface to the <b>stats</b> -function <code>sd</code> — see <a href="#">sd</a> resp. <code>help(sd, package="stats")</code> .
<code>sd, signature(x = "NormParameter")</code> :	returns the slot <code>sd</code> of the parameter of a normal distribution — see <a href="#">sd</a> resp. <code>help(sd, package="distr")</code> .
<code>sd, signature(x = "Norm")</code> :	returns the slot <code>sd</code> of the parameter of a normal distribution — see <a href="#">sd</a> resp. <code>help(sd, package="distr")</code> .
<code>sd, signature(x = "UnivariateDistribution")</code> :	standard deviation of univariate distributions using corresponding <code>E()</code> -method.
<code>IQR, signature(x = "Any")</code> :	interface to the <b>stats</b> -function <code>IQR</code> — see <a href="#">IQR</a> resp. <code>help(IQR, package="stats")</code> .
<code>IQR, signature(x = "UnivariateDistribution")</code> :	interquartile range of univariate distributions using corresponding <code>q()</code> -method.
<code>IQR, signature(x = "UnivariateCondDistribution")</code> :	interquartile range of univariate conditional distributions using corresponding <code>q()</code> -method.
<code>IQR, signature(x = "DiscreteDistribution")</code> :	interquartile range of discrete distributions using corresponding <code>q()</code> -method but taking care that between upper and lower quartile there is 50% probability
<code>IQR, signature(x = "AffLinDistribution")</code> :	$abs(x@a) * IQR(x@X0)$
<code>median, signature(x = "Any")</code> :	interface to the <b>stats</b> -function <code>median</code> — see <a href="#">median</a> resp. <code>help(var, package="stats")</code> .
<code>median, signature(x = "UnivariateDistribution")</code> :	median of univariate distributions using corresponding <code>q()</code> -method.

```

median, signature(x = "UnivariateCondDistribution"): median of univariate conditional dis-
tributions using corresponding q()-method.

median, signature(x = "AffLinDistribution"): x@a * median(x@X0) + x@b

mad, signature(x = "Any"): interface to the stats-function mad — see mad.

mad, signature(x = "UnivariateDistribution"): mad of univariate distributions using corre-
sponding q()-method applied to abs(x-median(x)).

mad, signature(x = "AffLinDistribution"): abs(x@a) * mad(x@X0)

skewness, signature(x = "Any"): bias free estimation of skewness under normal distribution (de-
fault) as well as sample version (by argument sample.version = TRUE).

skewness, signature(x = "UnivariateDistribution"): skewness of univariate distributions us-
ing corresponding E()-method.

skewness, signature(x = "AffLinDistribution"): if arguments fun, cond are missing: skewness(x@X0)
else uses method for signature(x = "UnivariateDistribution")

kurtosis, signature(x = "Any"): bias free estimation of kurtosis under normal distribution (de-
fault) as well as sample version (by argument sample.version = TRUE).

kurtosis, signature(x = "UnivariateDistribution"): kurtosis of univariate distributions us-
ing corresponding E()-method.

kurtosis, signature(x = "AffLinDistribution"): if arguments fun, cond are missing: kurtosis(x@X0)
else uses method for signature(x = "UnivariateDistribution")

var, signature(x = "Arcsine"): exact evaluation using explicit expressions.

var, signature(x = "Beta"): for noncentrality 0 exact evaluation using explicit expressions.

var, signature(x = "Binom"): exact evaluation using explicit expressions.

var, signature(x = "Cauchy"): exact evaluation using explicit expressions.

var, signature(x = "Chisq"): exact evaluation using explicit expressions.

var, signature(x = "Dirac"): exact evaluation using explicit expressions.

var, signature(x = "DExp"): exact evaluation using explicit expressions.

var, signature(x = "Exp"): exact evaluation using explicit expressions.

var, signature(x = "Fd"): exact evaluation using explicit expressions.

var, signature(x = "Gammad"): exact evaluation using explicit expressions.

var, signature(x = "Geom"): exact evaluation using explicit expressions.

var, signature(x = "Hyper"): exact evaluation using explicit expressions.

var, signature(x = "Logis"): exact evaluation using explicit expressions.

var, signature(x = "Lnorm"): exact evaluation using explicit expressions.

var, signature(x = "Nbinom"): exact evaluation using explicit expressions.

var, signature(x = "Norm"): exact evaluation using explicit expressions.

var, signature(x = "Pois"): exact evaluation using explicit expressions.

var, signature(x = "Td"): exact evaluation using explicit expressions.

var, signature(x = "Unif"): exact evaluation using explicit expressions.

var, signature(x = "Weibull"): exact evaluation using explicit expressions.

```

IQR, signature(x = "Arcsine"): exact evaluation using explicit expressions.  
IQR, signature(x = "Cauchy"): exact evaluation using explicit expressions.  
IQR, signature(x = "Dirac"): exact evaluation using explicit expressions.  
IQR, signature(x = "DExp"): exact evaluation using explicit expressions.  
IQR, signature(x = "Exp"): exact evaluation using explicit expressions.  
IQR, signature(x = "Geom"): exact evaluation using explicit expressions.  
IQR, signature(x = "Logis"): exact evaluation using explicit expressions.  
IQR, signature(x = "Norm"): exact evaluation using explicit expressions.  
IQR, signature(x = "Unif"): exact evaluation using explicit expressions.  
median, signature(x = "Arcsine"): exact evaluation using explicit expressions.  
median, signature(x = "Cauchy"): exact evaluation using explicit expressions.  
median, signature(x = "Dirac"): exact evaluation using explicit expressions.  
median, signature(x = "DExp"): exact evaluation using explicit expressions.  
median, signature(x = "Exp"): exact evaluation using explicit expressions.  
median, signature(x = "Geom"): exact evaluation using explicit expressions.  
median, signature(x = "Logis"): exact evaluation using explicit expressions.  
median, signature(x = "Lnorm"): exact evaluation using explicit expressions.  
median, signature(x = "Norm"): exact evaluation using explicit expressions.  
median, signature(x = "Unif"): exact evaluation using explicit expressions.  
mad, signature(x = "Arcsine"): exact evaluation using explicit expressions.  
mad, signature(x = "Cauchy"): exact evaluation using explicit expressions.  
mad, signature(x = "Dirac"): exact evaluation using explicit expressions.  
mad, signature(x = "DExp"): exact evaluation using explicit expressions.  
mad, signature(x = "Exp"): exact evaluation using explicit expressions.  
mad, signature(x = "Geom"): exact evaluation using explicit expressions.  
mad, signature(x = "Logis"): exact evaluation using explicit expressions.  
mad, signature(x = "Norm"): exact evaluation using explicit expressions.  
mad, signature(x = "Unif"): exact evaluation using explicit expressions.  
skewness, signature(x = "Arcsine"): exact evaluation using explicit expressions.  
skewness, signature(x = "Beta"): for noncentrality 0 exact evaluation using explicit expressions.  
skewness, signature(x = "Binom"): exact evaluation using explicit expressions.  
skewness, signature(x = "Cauchy"): exact evaluation using explicit expressions.  
skewness, signature(x = "Chisq"): exact evaluation using explicit expressions.  
skewness, signature(x = "Dirac"): exact evaluation using explicit expressions.  
skewness, signature(x = "DExp"): exact evaluation using explicit expressions.  
skewness, signature(x = "Exp"): exact evaluation using explicit expressions.

```

skewness, signature(x = "Fd"): exact evaluation using explicit expressions.
skewness, signature(x = "Gammad"): exact evaluation using explicit expressions.
skewness, signature(x = "Geom"): exact evaluation using explicit expressions.
skewness, signature(x = "Hyper"): exact evaluation using explicit expressions.
skewness, signature(x = "Logis"): exact evaluation using explicit expressions.
skewness, signature(x = "Lnorm"): exact evaluation using explicit expressions.
skewness, signature(x = "Nbinom"): exact evaluation using explicit expressions.
skewness, signature(x = "Norm"): exact evaluation using explicit expressions.
skewness, signature(x = "Pois"): exact evaluation using explicit expressions.
skewness, signature(x = "Td"): exact evaluation using explicit expressions.
skewness, signature(x = "Unif"): exact evaluation using explicit expressions.
skewness, signature(x = "Weibull"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Arcsine"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Beta"): for noncentrality 0 exact evaluation using explicit expressions.
kurtosis, signature(x = "Binom"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Cauchy"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Chisq"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Dirac"): exact evaluation using explicit expressions.
kurtosis, signature(x = "DExp"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Exp"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Fd"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Gammad"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Geom"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Hyper"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Logis"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Lnorm"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Nbinom"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Norm"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Pois"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Td"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Unif"): exact evaluation using explicit expressions.
kurtosis, signature(x = "Weibull"): exact evaluation using explicit expressions.

```

### Caveat

If any of the packages **e1071**, **moments**, **fBasics** is to be used together with **distrEx** the latter must be attached *after* any of the first mentioned. Otherwise **kurtosis()** and **skewness()** defined as *methods* in **distrEx** may get masked.

To re-mask, you may use `kurtosis <- distrEx::kurtosis; skewness <- distrEx::skewness.`  
See also `distrExMASK()`.

## Acknowledgement

G. Jay Kerns, <gkerns@ysu.edu>, has provided a major contribution, in particular the functionals skewness and kurtosis are due to him.

## Author(s)

Peter Ruckdeschel <peter.ruckdeschel@uni-oldenburg.de>

## See Also

[distrExIntegrate](#), [m1df](#), [m2df](#), [Distribution-class](#),  
[sd](#), [var](#), [IQR](#),  
[median](#), [mad](#), [sd](#),  
[Sn](#), [Qn](#)

## Examples

```
# Variance of Exp(1) distribution
var(Exp())

#median(Exp())
IQR(Exp())
mad(Exp())

# Variance of N(1,4)^2
var(Norm(mean=1, sd=2), fun = function(x){x^2})
var(Norm(mean=1, sd=2), fun = function(x){x^2}, useApply = FALSE)

## sd -- may equivalently be replaced by var
sd(Pois()) ## uses explicit terms
sd(as(Pois(),"DiscreteDistribution")) ## uses sums
sd(as(Pois(),"UnivariateDistribution")) ## uses simulations
sd(Norm(mean=2), fun = function(x){2*x^2}) ## uses simulations
#
mad(sin(exp(Norm()+2*Pois()))) ## weird
```

# Index

- \* **E**
  - distrEx-package, 2
- \* **IQR**
  - distrEx-package, 2
  - var, 65
- \* **S4 condition class**
  - Condition-class, 11
  - distrEx-package, 2
  - EuclCondition, 37
  - EuclCondition-class, 38
  - PrognCondition-class, 60
- \* **S4 distribution class**
  - AbscontCondDistribution-class, 6
  - ConvexContamination, 13
  - DiscreteCondDistribution-class, 16
  - DiscreteMVDistribution, 18
  - DiscreteMVDistribution-class, 19
  - distrEx-package, 2
  - EmpiricalMVDistribution, 36
  - LMCondDistribution, 46
  - MultivariateDistribution-class, 53
  - PrognCondDistribution, 58
  - PrognCondDistribution-class, 59
- \* **S4 linear model class**
  - LMPParameter-class, 48
- \* **S4 parameter class**
  - LMPParameter, 47
  - LMPParameter-class, 48
- \* **absolutely continuous distribution**
  - AbscontCondDistribution-class, 6
- \* **absolutely continuous distribution**
  - ConvexContamination, 13
- \* **accessor function**
  - dim-methods, 16
- \* **centering**
  - make01, 52
- \* **conditional distribution**
  - AbscontCondDistribution-class, 6
  - Condition-class, 11
- \* **DiscreteCondDistribution-class**, 16
- \* **distrEx-package**, 2
- \* **EuclCondition**, 37
- \* **EuclCondition-class**, 38
- \* **LMCondDistribution**, 46
- \* **PrognCondDistribution**, 58
- \* **PrognCondDistribution-class**, 59
- \* **PrognCondition-class**, 60
- \* **UnivariateCondDistribution-class**, 64
- \* **conditional expectation**
  - E, 26
- \* **conditioning**
  - Condition-class, 11
  - EuclCondition, 37
  - EuclCondition-class, 38
  - PrognCondition-class, 60
- \* **condition**
  - Condition-class, 11
  - EuclCondition, 37
  - EuclCondition-class, 38
  - PrognCondition-class, 60
- \* **convex contamination**
  - ContaminationSize, 12
  - ConvexContamination, 13
- \* **dimension**
  - dim-methods, 16
- \* **discrete distribution**
  - ConvexContamination, 13
  - DiscreteCondDistribution-class, 16
  - DiscreteMVDistribution, 18
  - DiscreteMVDistribution-class, 19
- \* **distance**
  - AsymTotalVarDist, 7
  - ContaminationSize, 12
  - CvMDist, 14
  - HellingerDist, 40
  - KolmogorovDist, 43
  - OAsymTotalVarDist, 54

TotalVarDist, 61  
\* **distribution distance**  
  distrEx-package, 2  
\* **distribution**  
  AbscontCondDistribution-class, 6  
  AsymTotalVarDist, 7  
  Condition-class, 11  
  ContaminationSize, 12  
  ConvexContamination, 13  
  CvMDist, 14  
  DiscreteCondDistribution-class, 16  
  DiscreteMVDistribution, 18  
  DiscreteMVDistribution-class, 19  
  distrExMASK, 23  
  distrExMOVED, 23  
  distrExOptions, 24  
  E, 26  
  EmpiricalMVDistribution, 36  
  EuclCondition, 37  
  EuclCondition-class, 38  
  HellingerDist, 40  
  KolmogorovDist, 43  
  liesInSupport, 45  
  LMCondDistribution, 46  
  LMPParameter-class, 48  
  m1df, 49  
  m2df, 50  
  make01, 52  
  MultivariateDistribution-class, 53  
  OAsymTotalVarDist, 54  
  PrognCondDistribution, 58  
  PrognCondDistribution-class, 59  
  PrognCondition-class, 60  
  TotalVarDist, 61  
  UnivariateCondDistribution-class,  
    64  
  var, 65  
\* **documentation**  
  distrExMASK, 23  
  distrExMOVED, 23  
\* **empirical distribution**  
  EmpiricalMVDistribution, 36  
\* **expectation**  
  E, 26  
\* **functional**  
  distrEx-package, 2  
  E, 26  
  m1df, 49  
  m2df, 50  
  make01, 52  
  var, 65  
\* **generating function**  
  DiscreteMVDistribution, 18  
  EmpiricalMVDistribution, 36  
  EuclCondition, 37  
  LMCondDistribution, 46  
  LMPParameter, 47  
  PrognCondDistribution, 58  
\* **global options**  
  distrExOptions, 24  
\* **gross error**  
  ContaminationSize, 12  
  ConvexContamination, 13  
\* **info file**  
  distrExMASK, 23  
  distrExMOVED, 23  
\* **integration**  
  distrExIntegrate, 20  
  E, 26  
  GLIntegrate, 39  
  var, 65  
\* **kurtosis**  
  distrEx-package, 2  
  var, 65  
\* **mad**  
  distrEx-package, 2  
  var, 65  
\* **masking**  
  distrExMASK, 23  
\* **math**  
  distrExIntegrate, 20  
  GLIntegrate, 39  
\* **median**  
  distrEx-package, 2  
  var, 65  
\* **methods**  
  ConvexContamination, 13  
  dim-methods, 16  
  E, 26  
  liesInSupport, 45  
  m1df, 49  
  m2df, 50  
  var, 65  
\* **misc**  
  distrExOptions, 24  
\* **models**

**\* moment**  
 E, 26  
 m1df, 49  
 m2df, 50

**\* moved functionality**  
 distrExMOVED, 23

**\* multivariate distribution**  
 DiscreteMVDistribution, 18  
 DiscreteMVDistribution-class, 19  
 distrEx-package, 2  
 EmpiricalMVDistribution, 36  
 MultivariateDistribution-class, 53

**\* options**  
 distrExOptions, 24

**\* package**  
 distrEx-package, 2

**\* parameter**  
 LMPParameter, 47  
 LMPParameter-class, 48

**\* prediction distribution**  
 PrognCondition-class, 60

**\* programming**  
 distrExMASK, 23  
 distrExMOVED, 23

**\* sd**  
 var, 65

**\* skewness**  
 distrEx-package, 2  
 var, 65

**\* space**  
 dim-methods, 16

**\* standardization**  
 make01, 52

**\* support**  
 liesInSupport, 45

**\* truncated moment**  
 m1df, 49  
 m2df, 50

**\* univariate distribution**  
 ConvexContamination, 13

**\* utilities**  
 distrExIntegrate, 20  
 GLIntegrate, 39  
 liesInSupport, 45

**\* var**  
 distrEx-package, 2

var, 65  
 .qtlIntegrate (E), 26  
 .reorganizeDiagnosticList, 21

AbscontCondDistribution-class, 6  
 AsymTotalVarDist, 7  
 AsymTotalVarDist, AbscontDistribution, AbscontDistribution-m  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, AbscontDistribution, DiscreteDistribution-  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, AbscontDistribution, numeric-method  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, AcDcLcDistribution, AcDcLcDistribution-m  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, DiscreteDistribution, AbscontDistribution-  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, DiscreteDistribution, DiscreteDistribution-  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, DiscreteDistribution, LatticeDistribution-  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, DiscreteDistribution, numeric-method  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, LatticeDistribution, DiscreteDistribution-  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, LatticeDistribution, LatticeDistribution-m  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, numeric, AbscontDistribution-method  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist, numeric, DiscreteDistribution-method  
     (AsymTotalVarDist), 7  
 AsymTotalVarDist-methods  
     (AsymTotalVarDist), 7

cond  
     (UnivariateCondDistribution-class),  
     64

cond, UnivariateCondDistribution-method  
     (UnivariateCondDistribution-class),  
     64

Condition-class, 11  
 ContaminationSize, 11, 12, 14, 16, 42, 44,  
     57, 64

ContaminationSize, AbscontDistribution, AbscontDistribution-  
     (ContaminationSize), 12

ContaminationSize, AcDcLcDistribution, AcDcLcDistribution-m  
     (ContaminationSize), 12

ContaminationSize, DiscreteDistribution, DiscreteDistribution-  
     (ContaminationSize), 12



E,Hyper,missing,missing-method (E), 26  
 E,LatticeDistribution,function,missing-methodUpperTruncQuantile (distrExOptions), 24  
     (E), 26  
 E,LatticeDistribution,missing,missing-method getDiagnostic, 10, 15, 32, 42, 56, 63  
     (E), 26  
 E,Lnorm,missing,missing-method getDiagnostic (distrExIntegrate), 20  
 E,Logis,missing,missing-method getoptdistrExOption (distrExOptions), 24  
 E,MultivariateDistribution,function,missing-methodgetOption, 25  
     (E), 26  
 E,MultivariateDistribution,missing,missing-methodgetIntegrate, 22, 39  
     (E), 26  
 GLIntegrateOrder (distrExOptions), 24  
 E,MultivariateDistribution,missing,missing-methodgetIntegrateTruncQuantile  
     (E), 26  
 (distrExOptions), 24  
 E,Nbinom,missing,missing-method (E), 26  
 E,Norm,missing,missing-method (E), 26  
 HellingerDist, 11, 13, 16, 40, 44, 57, 64  
 E,Pois,missing,missing-method (E), 26  
 HellingerDist,AbscontDistribution,AbscontDistribution-method  
 E,Td,missing,missing-method (E), 26  
     (HellingerDist), 40  
 E,Unif,missing,missing-method (E), 26  
 HellingerDist,AbscontDistribution,DiscreteDistribution-method  
 E,UnivariateCondDistribution,function,numeric-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,AbscontDistribution,numeric-method  
 E,UnivariateCondDistribution,missing,numeric-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,AcDcLcDistribution,AcDcLcDistribution-method  
 E,UnivariateDistribution,function,missing-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,DiscreteDistribution,AbscontDistribution-method  
 E,UnivariateDistribution,missing,missing-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,DiscreteDistribution,DiscreteDistribution-method  
 E,UnivarLebDecDistribution,function,ANY-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,DiscreteDistribution,LatticeDistribution-method  
 E,UnivarLebDecDistribution,function,missing-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,DiscreteDistribution,numeric-method  
 E,UnivarLebDecDistribution,missing,ANY-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,DiscreteMVDistribution,DiscreteMVDistribution  
 E,UnivarLebDecDistribution,missing,missing-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,LatticeDistribution,DiscreteDistribution-method  
 E,UnivarMixingDistribution,function,ANY-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,LatticeDistribution,LatticeDistribution-method  
 E,UnivarMixingDistribution,function,missing-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,numeric,AbscontDistribution-method  
 E,UnivarMixingDistribution,missing,ANY-method (HellingerDist), 40  
     (E), 26  
 HellingerDist,numeric,DiscreteDistribution-method  
 E,UnivarMixingDistribution,missing,missing-method (HellingerDist), 40  
     (E), 26  
 HellingerDist-methods (HellingerDist), 40  
 E,Weibull,function,missing-method (E),  
     26  
 hSmooth (distrExOptions), 24  
 E,Weibull,missing,missing-method (E), 26  
 E-methods (E), 26  
 IQR, 71, 75  
 ElowerTruncQuantile (distrExOptions), 24  
 EmpiricalMVDistribution, 36  
 ErelativeTolerance (distrExOptions), 24  
 EuclCondition, 37, 38  
 integrate, 22, 39  
 IQR (var), 65  
 IQR,AffLinAbscontDistribution-method  
     (var), 65

IQR, AffLinDiscreteDistribution-method  
     (var), 65

IQR, AffLinDistribution-method (var), 65

IQR, AffLinLatticeDistribution-method  
     (var), 65

IQR, ANY-method (var), 65

IQR, Arcsine-method (var), 65

IQR, Cauchy-method (var), 65

IQR, DExp-method (var), 65

IQR, Dirac-method (var), 65

IQR, DiscreteDistribution-method (var),  
     65

IQR, Exp-method (var), 65

IQR, Geom-method (var), 65

IQR, Logis-method (var), 65

IQR, Norm-method (var), 65

IQR, Unif-method (var), 65

IQR, UnivariateCondDistribution-method  
     (var), 65

IQR, UnivariateDistribution-method  
     (var), 65

IQR-methods (var), 65

IQR.fac (distrExOptions), 24

KolmogorovDist, 11, 13, 16, 42, 43, 57, 64

KolmogorovDist, AbscontDistribution, AbscontDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, AbscontDistribution, DiscreteDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, AcDcLcDistribution, AcDcLcDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, DiscreteDistribution, AbscontDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, DiscreteDistribution, DiscreteDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, DiscreteDistribution, DiscreteDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, DiscreteDistribution, LatticeDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, LatticeDistribution, DiscreteDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, LatticeDistribution, LatticeDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, numeric, UnivariateDistribution-method  
     (KolmogorovDist), 43

KolmogorovDist, UnivariateDistribution, numeric-method 49  
     (KolmogorovDist), 43

KolmogorovDist-methods  
     (KolmogorovDist), 43

kurtosis (var), 65

kurtosis, AffLinAbscontDistribution-method  
     (var), 65

kurtosis, AffLinDiscreteDistribution-method  
     (var), 65

kurtosis, AffLinDistribution-method  
     (var), 65

kurtosis, AffLinLatticeDistribution-method  
     (var), 65

kurtosis, ANY-method (var), 65

kurtosis, Arcsine-method (var), 65

kurtosis, Beta-method (var), 65

kurtosis, Binom-method (var), 65

kurtosis, Cauchy-method (var), 65

kurtosis, Chisq-method (var), 65

kurtosis, DExp-method (var), 65

kurtosis, Dirac-method (var), 65

kurtosis, Exp-method (var), 65

kurtosis, Fd-method (var), 65

kurtosis, Gammad-method (var), 65

kurtosis, Geom-method (var), 65

kurtosis, Hyper-method (var), 65

kurtosis, Lnorm-method (var), 65

kurtosis, Logis-method (var), 65

kurtosis, Nbinom-method (var), 65

kurtosis, Norm-method (var), 65

kurtosis, Pois-method (var), 65

kurtosis, Td-method (var), 65

kurtosis, Unif-method (var), 65

Kurtosis, UnivariateDistribution-method  
     (var), 65

Kurtosis, Weibull-method (var), 65

kurtosis-methods (var), 65

liesInSupport, 45

liesInSupport, DiscreteMVDistribution, matrix-method  
     (liesInSupport), 45

liesInSupport, DiscreteMVDistribution, numeric-method  
     (liesInSupport), 45

EMCONDIST10U10n, 46

LMPParameter, 47, 48

LMPParameter-class, 48

m1df, 49, 75

m1df, AbscontDistribution-method (m1df),  
     49

m1df, AffLinDistribution-method (m1df),  
     49

m1df, Binom-method (m1df), 49

m1df, Chisq-method (m1df), 49

`m1df`, `Exp-method (m1df)`, 49  
`m1df`, `LatticeDistribution-method (m1df)`, 49  
`m1df`, `Norm-method (m1df)`, 49  
`m1df`, `Pois-method (m1df)`, 49  
`m1df`, `UnivariateDistribution-method (m1df)`, 49  
`m1df-methods (m1df)`, 49  
`m1dfLowerTruncQuantile (distrExOptions)`, 24  
`m1dfRelativeTolerance (distrExOptions)`, 24  
`m2df`, 35, 50, 50, 75  
`m2df`, `AbscontDistribution-method (m2df)`, 50  
`m2df`, `AffLinDistribution-method (m2df)`, 50  
`m2df`, `Binom-method (m2df)`, 50  
`m2df`, `Chisq-method (m2df)`, 50  
`m2df`, `Exp-method (m2df)`, 50  
`m2df`, `LatticeDistribution-method (m2df)`, 50  
`m2df`, `Norm-method (m2df)`, 50  
`m2df`, `Pois-method (m2df)`, 50  
`m2df`, `UnivariateDistribution-method (m2df)`, 50  
`m2df-methods (m2df)`, 50  
`m2dfLowerTruncQuantile (distrExOptions)`, 24  
`m2dfRelativeTolerance (distrExOptions)`, 24  
`mad`, 72, 75  
`mad (var)`, 65  
`mad`, `AffLinAbscontDistribution-method (var)`, 65  
`mad`, `AffLinDiscreteDistribution-method (var)`, 65  
`mad`, `AffLinDistribution-method (var)`, 65  
`mad`, `AffLinLatticeDistribution-method (var)`, 65  
`mad`, `ANY-method (var)`, 65  
`mad`, `Arcsine-method (var)`, 65  
`mad`, `Cauchy-method (var)`, 65  
`mad`, `DExp-method (var)`, 65  
`mad`, `Dirac-method (var)`, 65  
`mad`, `Exp-method (var)`, 65  
`mad`, `Geom-method (var)`, 65  
`mad`, `Logis-method (var)`, 65

`mad`, `Norm-method (var)`, 65  
`mad`, `Unif-method (var)`, 65  
`mad`, `UnivariateDistribution-method (var)`, 65  
`mad-methods (var)`, 65  
`make01`, 52  
`MASKING (distrExMASK)`, 23  
`MCIterations (distrExOptions)`, 24  
`median`, 71, 75  
`median (var)`, 65  
`median`, `AffLinAbscontDistribution-method (var)`, 65  
`median`, `AffLinDiscreteDistribution-method (var)`, 65  
`median`, `AffLinDistribution-method (var)`, 65  
`median`, `AffLinLatticeDistribution-method (var)`, 65  
`median`, `ANY-method (var)`, 65  
`median`, `Arcsine-method (var)`, 65  
`median`, `Cauchy-method (var)`, 65  
`median`, `DExp-method (var)`, 65  
`median`, `Dirac-method (var)`, 65  
`median`, `Exp-method (var)`, 65  
`median`, `Geom-method (var)`, 65  
`median`, `Lnorm-method (var)`, 65  
`median`, `Logis-method (var)`, 65  
`median`, `Norm-method (var)`, 65  
`median`, `Unif-method (var)`, 65  
`median`, `UnivariateCondDistribution-method (var)`, 65  
`median`, `UnivariateDistribution-method (var)`, 65  
`median-methods (var)`, 65  
`MOVEDING (distrExMOVED)`, 23  
`MultivariateDistribution-class`, 53  
`name`, `Condition-method (Condition-class)`, 11  
`name<-`, `Condition-method (Condition-class)`, 11  
`nDiscretize (distrExOptions)`, 24  
`OAsymTotalVarDist`, 54  
`OAsymTotalVarDist`, `AbscontDistribution, AbscontDistribution- (OAsymTotalVarDist)`, 54  
`OAsymTotalVarDist`, `AbscontDistribution, DiscreteDistribution (OAsymTotalVarDist)`, 54

0AsymTotalVarDist, *AbscontDistribution*, numeric-method  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *AcDclcDistribution*, *AcDlcDistribution*-method  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *DiscreteDistribution*, *AbscontDistribution*-method  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *DiscreteDistribution*, *DiscreteDistribution*-method  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *DiscreteDistribution*, *LatticeDistribution*  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *DiscreteDistribution*, numeric-method  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *LatticeDistribution*, *DiscreteDistribution*-method  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, *LatticeDistribution*, *LatticeDistribution*  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, numeric, *AbscontDistribution*  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist, numeric, *DiscreteDistribution*  
     (*OAsymTotalVarDist*), 54  
 0AsymTotalVarDist-methods  
     (*OAsymTotalVarDist*), 54  
 options, 25  
 plot (plot-methods), 57  
 plot, *MultivariateDistribution*, missing-method  
     (plot-methods), 57  
 plot, *MultivariateDistribution*-method  
     (*MultivariateDistribution*-class), 53  
 plot, *UnivariateCondDistribution*, missing-method  
     (plot-methods), 57  
 plot, *UnivariateCondDistribution*-method  
     (*UnivariateCondDistribution*-class), 64  
 plot-methods, 57  
 print.DiagnosticClass  
     (*distrExIntegrate*), 20  
 PrognCondDistribution, 58, 59  
 PrognCondDistribution-class, 59  
 PrognCondition (*PrognCondition*-class), 60  
 PrognCondition-class, 60  
 propagate.names.functionals  
     (*distrExOptions*), 24  
 Qn, 75  
 Range (*EuclCondition*-class), 38

Range, *EuclCondition*-method  
     (*EuclCondition*-class), 38  
 sd, 71, 75  
 sd, var, 65  
 sd, Norm-method (var), 65  
 sd, MultivariateDistribution-method (var), 65  
 sd, methods for var, 65  
 show, *EuclCondition*-method  
 show, LMPParameter-method  
 show, (*LMPParameter*-class), 48  
 show, MultivariateDistribution-method  
 show, (*MultivariateDistribution*-class), 53  
 show, PrognCondition-method  
     (*PrognCondition*-class), 60  
 show, UnivariateCondDistribution-method  
     (*UnivariateCondDistribution*-class), 64  
 showDiagnostic, 10, 15, 32, 42, 56, 63  
 showDiagnostic (*distrExIntegrate*), 20  
 skewness (var), 65  
 skewness, *AffLinAbscontDistribution*-method  
     (var), 65  
 skewness, *AffLinDiscreteDistribution*-method  
     (var), 65  
 skewness, *AffLinDistribution*-method  
     (var), 65  
 skewness, *AffLinLatticeDistribution*-method  
     (var), 65  
 skewness, ANY-method (var), 65  
 skewness, Arcsine-method (var), 65  
 skewness, Beta-method (var), 65  
 skewness, Binom-method (var), 65  
 skewness, Cauchy-method (var), 65  
 skewness, Chisq-method (var), 65  
 skewness, DExp-method (var), 65  
 skewness, Dirac-method (var), 65  
 skewness, Exp-method (var), 65  
 skewness, Fd-method (var), 65  
 skewness, Gammad-method (var), 65  
 skewness, Geom-method (var), 65  
 skewness, Hyper-method (var), 65  
 skewness, Lnorm-method (var), 65  
 skewness, Logis-method (var), 65  
 skewness, Nbinom-method (var), 65  
 skewness, Norm-method (var), 65

skewness, Pois-method (var), 65  
 skewness, Td-method (var), 65  
 skewness, Unif-method (var), 65  
 skewness, UnivariateDistribution-method (var), 65  
 skewness, Weibull-method (var), 65  
 skewness-methods (var), 65  
 Sn, 75  
 support, DiscreteMVDistribution-method (DiscreteMVDistribution-class), 19  
  
 TotalVarDist, 13, 16, 42, 44, 61  
 TotalVarDist, AbscontDistribution, AbscontDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, AbscontDistribution, DiscreteDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, AbscontDistribution, numeric-method (TotalVarDist), 61  
  
 TotalVarDist, AcDcLcDistribution, AcDcLcDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, DiscreteDistribution, AbscontDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, DiscreteDistribution, DiscreteDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, DiscreteDistribution, LatticeDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, DiscreteDistribution, numeric-method (TotalVarDist), 61  
  
 TotalVarDist, DiscreteMVDistribution, DiscreteMVDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, LatticeDistribution, DiscreteDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, LatticeDistribution, LatticeDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, numeric, AbscontDistribution-method (TotalVarDist), 61  
  
 TotalVarDist, numeric, DiscreteDistribution-method (TotalVarDist), 61  
  
 TotalVarDist-methods (TotalVarDist), 61  
  
 UnivariateCondDistribution-class, 64  
  
 var, 65, 71, 75  
 var, AffLinAbscontDistribution-method (var), 65  
 var, AffLinDiscreteDistribution-method (var), 65  
 var, AffLinDistribution-method (var), 65  
 var, AffLinLatticeDistribution-method (var), 65  
 var, ANY-method (var), 65  
 var, Arcsine-method (var), 65  
 var, Beta-method (var), 65  
 var, Binom-method (var), 65  
 var, Cauchy-method (var), 65  
 var, Chisq-method (var), 65  
 var, CompoundDistribution-method (var), 65  
 var, DExp-method (var), 65  
 var, Dirac-method (var), 65  
 var, Exp-method (var), 65  
 var, Gamma-method (var), 65  
 var, Geom-method (var), 65  
 var, Hyper-method (var), 65  
 var, Lnorm-method (var), 65  
 var, Logis-method (var), 65  
 var, Norm-method (var), 65  
 var, Pois-method (var), 65  
 var, Td-method (var), 65  
 var, UnivariateDistribution-method (var), 65  
 var, Weibull-method (var), 65