

# Package ‘gnonadd’

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**Type** Package

**Title** Various Non-Additive Models for Genetic Associations

**Version** 1.0.2

**Description** The goal of 'gnonadd' is to simplify workflows in the analysis of non-additive effects of sequence variants. This includes variance effects (Ivarsdottir et. al (2017) <[doi:10.1038/ng.3928](https://doi.org/10.1038/ng.3928)>), correlation effects, interaction effects and dominance effects. The package also includes convenience functions for visualization.

**URL** <https://github.com/DecodeGenetics/gnonadd>

**BugReports** <https://github.com/DecodeGenetics/gnonadd/issues>

**License** MIT + file LICENSE

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alpha.calc	<i>Genetic variance effects</i>
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**Description**

This function estimates the variance effect of a genetic variant on a quantitative trait. The genotype is coded as 0 (non-carrier), 1 (single copy of effect allele) and 2 (two copies of effect allele). The variance effect (alpha) is modelled to be multiplicative. We use a likelihood ratio test with 1 degree of freedom, \* H0:  $y \sim N(\mu_g, \sigma^2)$  \* H1:  $y \sim N(\mu_g, \sigma^2 * \alpha^g)$  Under the alternative model, the variance of the trait changes multiplicatively with genotype:  $\text{Var}(y|g=j) = \alpha^j * \sigma^2$ , j in 0,1,2

**Usage**

```
alpha.calc(qt, g)
```

**Arguments**

qt	A numeric vector.
g	An integer vector.

**Value**

A list with the values:

\* alpha, the estimated variance effect \* sigma2\_alt, The variance estimated for non-carriers \* pval, the p-value of the likelihood ratio test \* chi2, the chi squared statistics (with one degree of freedom) corresponding to the p-value

**Examples**

```
n_val <- 50000L
geno_vec <- sample(c(0, 1, 2), size = n_val, replace = TRUE)
qt_vec <- rnorm(n_val) * (1.1^geno_vec)
res <- alpha.calc(qt_vec, geno_vec)
```

alpha.cond

*Conditional analysis for genetic variance effects***Description**

We estimate the variance effect of a primary variant conditioned on one or more secondary variants. We apply a likelihood ratio test with one degree of freedom

H0: All secondary variants have a variance effect, but not the primary one. H1: All variants have a variance effect, including the primary one

Under both models we assume a full mean effect model. That is, the number of mean-value parameters is  $3^{(n+1)}$ , where  $n$  is the number of covariates. Thus the null model has  $3^{(n+1)}+n$  degrees of freedom whereas the alternative model has  $3^{(n+1)}+n+1$ . Due to the exponential growth of free parameters, the test might have low statistical power if many covariates are used

**IMPORTANT NOTE:** We use the Gauss-Newton algorithm to estimate many parameters. We do not check if the algorithm converges to the true minimum values, or if it converges at all. Thus, we advise against blindly believing all results

**Usage**

```
alpha.cond(qt, g, g_covar, iter_num = 50)
```

**Arguments**

qt	A numeric vector.
g	An integer vector.
g_covar	An integer matrix where each column corresponds to a genetic covariate
iter_num	An integer. Represents the number of iterations performed in the Gauss-Newton algorithm

**Value**

A list with the values: \* alpha, the estimated variance effect, conditioned on the covariates \* pval, the p-value corresponding to alpha

**Examples**

```

n <- 10000
qt <- rnorm(n)
g <- rbinom(n, 2, 0.3)
qt <- qt * 1.2^g
g_covar <- as.data.frame(matrix(0, nrow = n, ncol = 3))
for(i in 1:ncol(g_covar)){
  freq <- runif(1, min = 0, max = 1)
  g_covar[, i] <- rbinom(n, 2, freq)
}
res <- alpha.cond(qt, g, g_covar)

```

---

alpha.continuous.cond *variance effect conditioned on continuous variables*

---

**Description**

We estimate the variance effect of a variant conditioned on one or more continuous variable We apply a likelihood ratio test with one degree of freedom

H0: All covariates have a variance effect, but not the variant H1: The variant has a variance effect, and the covariates as well

**Usage**

```
alpha.continuous.cond(qt, g, x, iter_num = 50, eps_param = 1e-10)
```

**Arguments**

qt	A numeric vector.
g	An integer vector.
x	A numeric matrix, each column represents a covariate.
iter_num	An integer. Represents the number of iterations performed in the Gauss-Newton algorithm
eps_param	A number. The Gauss-Newton algorithm terminates if the increment change of all variance estimates is smaller than this number.

**Value**

A list with the values: \* alpha, the estimated variance effect, conditioned on the covariates \* pval, the p-value corresponding to alpha

**Examples**

```

n_val <- 50000
x <- matrix(0,nrow = n_val, ncol = 4)
for(i in 1:4) {
  x[, i] <- rnorm(n_val)
}
g_vec <- rbinom(n_val,2,0.3)
var_vec <- exp(0.2 * x[, 1] - 0.3 * x[, 4] + 0.3 * g_vec)
qt_vec <- rnorm(n_val, 0, sqrt(var_vec))
res <- alpha.continuous.cond(qt_vec, g_vec, x)

```

---

alpha.multi.est	<i>Variance parameters</i>
-----------------	----------------------------

---

**Description**

This function jointly estimates the variance effect of a set of (continuous) variables on a qt trait. More precisely. It finds the maximum likelihood estimators.

**Usage**

```

alpha.multi.est(
  qt,
  x,
  iter_num = 50,
  eps_param = 1e-10,
  initial_guess = rep(0, ncol(x))
)

```

**Arguments**

qt	A numeric vector.
x	A numeric matrix, each column represents a covariate.
iter_num	An integer. Represents the number of iterations performed in the Gauss-Newton algorithm
eps_param	A number. The Gauss-Newton algorithm terminates if the increment change of all variance estimates is smaller than this number.
initial_guess	A vector of length ncol(x). Represents the initial guess of parameters for the Gauss-Newton algorithm.

**Value**

A vector with a variance estimate for each variable.

**Examples**

```
n_val <- 50000
x <- matrix(0,nrow = n_val, ncol = 4)
for(i in 1:4) {
  x[, i] <- rnorm(n_val)
}
var_vec <- exp(0.2 * x[, 1] - 0.3 * x[, 4])
qt_vec <- rnorm(n_val, 0, sqrt(var_vec))
res <- alpha.multi.est(qt_vec, x)
```

---

 corr.calibration

*Calibration for the correlation test*


---

**Description**

This function finds appropriate scaling\_parameters for the kappa\_calc function by means of bootstrapping.

**Usage**

```
corr.calibration(qt1, qt2, reps = 10000)
```

**Arguments**

qt1	A numeric vector.
qt2	A numeric vector.
reps	The number of repeats we want to perform for each sample size

**Value**

A list with the values:

- \* bias\_scale, a value to determine the bias for the correlation estimators
- \* weight\_scale, a value to determine how much weight we assign to each correlation estimator
- \* safe\_weight\_scale, same as weight scale, but larger. Using this weight decreases the chance of type 1 error, with the cost of statistical power.

**Examples**

```
n_val <- 10000
Q <- MASS::mvrnorm(n = n_val, mu = c(0,0), Sigma = matrix(c(1,0.3,0.3,1),
  nrow = 2, ncol = 2))
qt1_val <- Q[,1]
qt2_val <- Q[,2]
res <- corr.calibration(qt1_val, qt2_val, 10)
```

---

dominance.calc      *Genetic dominance effects*

---

## Description

This function estimates the dominance effect of a genetic variant on a quantitative trait. Nothing fancy here. We apply a simple linear regression model to estimate dominance effects. We include a linear term, coded as 0, 1 and 2 for non-carriers, heterozygotes and homozygous carriers of the effect allele. We also include a dominance term, coded as 1 for homozygous carriers and 0 for others. Effect size and significance is based on the dominance term.

## Usage

```
dominance.calc(  
  qt,  
  g,  
  round_imputed = FALSE,  
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))  
)
```

## Arguments

qt	A numeric vector
g	A vector with (possibly imputed) genotype values. All entries should be larger than 0 and smaller than 2.
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis
covariates	A dataframe containing any covariates that should be used; one column per covariate.

## Value

A list with the dominance effect and corresponding standard error, t statistic and p-value

## Examples

```
g_vec <- rbinom(100000, 2, 0.3)  
qt_vec <- rnorm(100000) + 0.2 * g_vec^2  
res <- dominance.calc(qt_vec, g_vec)
```

---

dominance\_CC.calc      *Genetic dominance effects on a case control variable*

---

### Description

This function estimates the dominance effect of a genetic variant on a case-control variable. We apply a logistic regression model to estimate dominance effects. We include a linear term, coded as 0, 1 and 2 for non-carriers, heterozygotes and homozygous carriers of the effect allele. We also include a dominance term, coded as 1 for homozygous carriers and 0 for others. Effect size and significance is based on the dominance term.

### Usage

```
dominance_CC.calc(
  cc,
  g,
  yob = rep(-1, length(cc)),
  sex = rep(-1, length(cc)),
  round_imputed = FALSE,
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))
)
```

### Arguments

cc	A case control vector, containing 0's and 1's
g	A vector with (possibly imputed) genotype values. All entries should be larger than 0 and smaller than 2.
yob	A numerical vector containing year of birth. If some are unknown they should be marked as -1
sex	A numerical vector containing sex, coded 0 for males, 1 for females and -1 for unknown
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis
covariates	A dataframe containing any other covariates that should be used; one column per covariate.

### Value

A list with the dominance effect (on log-scale) and corresponding standard error, z statistic and p-value

### Examples

```
g_vec <- rbinom(100000, 2, 0.3)
cc_vec <- rbinom(100000, 1, 0.1 * (1.2 ^ (g_vec^2)))
res <- dominance_CC.calc(cc_vec, g_vec)
```

---

ellipse.by.gen      *Ellipse best fit plot*

---

## Description

This tool creates a scatter plot along with regression lines. Additionally it finds and plots the best ellipses that fit the data.

## Usage

```
ellipse.by.gen(  
  qt1,  
  qt2,  
  g,  
  trait_name1 = "qt trait 1",  
  trait_name2 = "qt trait 2",  
  title = "",  
  sample_size = 500  
)
```

## Arguments

qt1	A numeric vector.
qt2	A numeric vector.
g	An integer vector.
trait_name1	A string.
trait_name2	A string.
title	A string.
sample_size	A positive integer.

## Value

A scatter plot.

## Examples

```
n_val <- 10000L  
geno_vec <- c(rep(0, n_val), rep(1, n_val), rep(2, n_val))  
qt_g0 <- MASS::mvrnorm(n_val, mu = c(0, 0), Sigma = matrix(c(0.93, 0.88, 0.88, 0.92), ncol = 2))  
qt_g1 <- MASS::mvrnorm(n_val, mu = c(0, 0), Sigma = matrix(c(0.98, 0.88, 0.88, 0.90), ncol = 2))  
qt_g2 <- MASS::mvrnorm(n_val, mu = c(0, 0), Sigma = matrix(c(1.57, 0.81, 0.81, 0.59), ncol = 2))  
qt_vec <- rbind(qt_g0, qt_g1)  
qt_vec <- rbind(qt_vec, qt_g2)  
res <- ellipse.by.gen(qt_vec[, 1], qt_vec[, 2], geno_vec)
```

---

env\_interaction.calc    *Variant-Environmental interaction effects*

---

### Description

This function estimates the interaction effect of a genetic variant with an environmental factor on a quantitative trait. We apply a simple linear regression model to estimate interaction effects. We include a linear term for the variant and environmental variable separately. The variant is coded as 0, 1 and 2 for non-carriers, heterozygotes and homozygous carriers of the effect allele. The environmental variable is rank-normalized automatically as part of the function. The interaction term is defined as the product of the genetic and the (normalized) environmental variables. Effect size and significance is based on the interaction term.

### Usage

```
env_interaction.calc(  
  qt,  
  g,  
  env,  
  round_imputed = FALSE,  
  dominance_term = FALSE,  
  square_env = FALSE,  
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))  
)
```

### Arguments

qt	A numeric vector
g	A vector with (possibly imputed) genotype values. All entries should be larger than 0 and smaller than 2.
env	A numeric vector with an environmental variable
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_term	A boolean variable determining whether a dominance term for the variant should be included as a covariate in the analysis
square_env	A boolean variable determining whether the square of the environmental trait should be included as a covariate in the analysis
covariates	A dataframe containing any other covariates that should be used; one column per covariate

### Value

A list with the environmental interaction effect and corresponding standard error, t statistic and p-value

**Examples**

```
g_vec <- rbinom(100000, 2, 0.1)
env_vec <- round(runif(100000,min=0,max=6))
qt_vec <- rnorm(100000) + 0.1 * g_vec + 0.05 * env_vec + 0.05 * g_vec * env_vec
res <- env_interaction.calc(qt_vec, g_vec, env_vec)
```

---

env\_interaction\_CC.calc

*Variant-Environmental interaction effects on a case control variable*

---

**Description**

This function estimates the interaction effect of a genetic variant with an environmental factor on a case control variable. We apply a simple logistic regression model to estimate interaction effects. We include a linear term for the variant and environmental variable separately. The variant is coded as 0, 1 and 2 for non-carriers, heterozygotes and homozygous carriers of the effect allele. The environmental variable is rank-normalized automatically as part of the function. The interaction term is defined as the product of the genetic and the (normalized) environmental variable. Effect size and significance is based on the interaction term.

**Usage**

```
env_interaction_CC.calc(
  cc,
  g,
  env,
  yob = rep(-1, length(cc)),
  sex = rep(-1, length(cc)),
  round_imputed = FALSE,
  dominance_term = FALSE,
  square_env = FALSE,
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))
)
```

**Arguments**

cc	A numeric vector
g	A vector with (possibly imputed) genotype values. All entries should be larger than 0 and smaller than 2.
env	A numeric vector with an environmental variable
yob	A numerical vector containing year of birth. If some are unknown they should be marked as -1
sex	A numerical vector containing sex, coded 0 for males, 1 for females and -1 for unknown
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.

<code>dominance_term</code>	A boolean variable determining whether a dominance term for the variant should be included as a covariates in the analysis
<code>square_env</code>	A boolean variable determining whether the square of the environmental trait should be included as a covariate in the analysis
<code>covariates</code>	A dataframe containing any other covariates that should be used; one column per covariate

**Value**

A list with the environmental interaction effect and corresponding standard error, t statistic and p-value

**Examples**

```
g_vec <- rbinom(100000, 2, 0.9)
env_vec <- round(runif(100000, min = 0, max = 6))
cc_vec <- rbinom(100000, 1, 0.1 * (1.05^g_vec) *
  (1.1^env_vec) * (1.1 ^ (g_vec * env_vec)))
res <- env_interaction_CC.calc(cc_vec, g_vec, env_vec)
```

---

`expected.variance.effect`

*Expected variance effect from additive effect*

---

**Description**

This function interpolates data from a simple simulation to give an estimate of the variance effect induced by an additive effect. The simulation code is stored under `inst/raw/`. We assume that the trait has been inverse normal transformed. Under the simulation, there is no variance effect, so the variance effect is fully induced by the inverse normal transform.

**Usage**

```
expected.variance.effect(maf, beta_add)
```

**Arguments**

<code>maf</code>	Minor allele frequency of the variant, should be in the range 0 to 0.5.
<code>beta_add</code>	Additive effect of the variant, should be in the range 0 to 3.5. This variable can be a vector of values.

**Value**

The expected variance effect for the variant from the given maf, beta combination.

**Examples**

```
maf <- 0.1
beta_val <- 0.3
expected_var <- expected.variance.effect(maf, beta_val)

beta_vec <- seq(0.1,2, length.out = 20)
expected_var <- expected.variance.effect(maf, beta_vec)
```

---

hist_by_gen	<i>Histogram by genotype</i>
-------------	------------------------------

---

**Description**

This tool creates three histogram plots. One per genotype. Additionally, outliers are colored red (by default subjects that are in the top and bottom 2.5 and blue lines are added to indicate the mean and (by default) one standard deviation in each direction.

**Usage**

```
hist_by_gen(
  qt,
  g,
  bins = 100,
  trait_name = "qt trait",
  title = "",
  outlier_quantiles = c(0.025, 0.975),
  sd_lines = c(1, 1)
)
```

**Arguments**

qt	A numeric vector.
g	An integer vector.
bins	An integer.
trait_name	A string.
title	A string.
outlier_quantiles	A vector with length 2.
sd_lines	A vector with length 2.

**Value**

A histogram plot

**Examples**

```
n_val <- 50000L
geno_vec <- sample(c(0, 1, 2), size = n_val, replace = TRUE)
qt_vec <- rnorm(n_val) * (1.3^geno_vec) + 1 * geno_vec
hist_by_gen(qt_vec, geno_vec)
```

---

interaction.calc      *Variant-Variant interaction effects*

---

**Description**

This function estimates the interaction effect of a pair of genetic variant on a quantitative trait. We apply a simple linear regression model to estimate interaction effects. We include a linear term for each variant separately, coded as 0, 1 and 2 for non-carriers, heterozygotes and homozygous carriers of the effect allele. We also include an interaction term, coded as the product of the two genotype values. Effect size and significance is based on the interaction term.

**Usage**

```
interaction.calc(
  qt,
  g1,
  g2,
  round_imputed = FALSE,
  dominance_terms = FALSE,
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))
)
```

**Arguments**

qt	A numeric vector
g1	A vector with (possibly imputed) genotype values. All entries should be larger than or equal to 0 and smaller than or equal to 2.
g2	A vector with (possibly imputed) genotype values. All entries should be larger than or equal to 0 and smaller than or equal to 2.
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_terms	A boolean variable determining whether dominance terms for the variants should be included as covariates in the analysis
covariates	A dataframe containing any other covariates that should be used; one column per covariate

**Value**

A list with the interaction effect and corresponding standard error, t statistic and p-value

**Examples**

```
g1_vec <- rbinom(100000, 2, 0.9)
g2_vec <- rbinom(100000, 2, 0.1)
qt_vec <- rnorm(100000) + 0.1 * g1_vec + 0.2 * g2_vec + 0.4 * g1_vec * g2_vec
res <- interaction.calc(qt_vec, g1_vec, g2_vec)
```

---

interaction\_CC.calc     *Variant-Variant interaction effects on a case control variable*

---

**Description**

This function estimates the interaction effect of a pair of genetic variant on a case-control variable. We apply a logistic regression model to estimate interaction effects. We include a linear term for each variant separately, coded as 0, 1 and 2 for non-carriers, heterozygotes and homozygous carriers of the effect allele. We also include an interaction term, coded as the product of the two genotype values. Effect size and significance is based on the interaction term.

**Usage**

```
interaction_CC.calc(
  cc,
  g1,
  g2,
  yob = rep(-1, length(cc)),
  sex = rep(-1, length(cc)),
  round_imputed = FALSE,
  dominance_terms = FALSE,
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))
)
```

**Arguments**

cc	A numeric vector
g1	A vector with (possibly imputed) genotype values. All entries should be larger than 0 and smaller than 2.
g2	A vector with (possibly imputed) genotype values. All entries should be larger than 0 and smaller than 2.
yob	A numerical vector containing year of birth. If some are unknown they should be marked as -1
sex	A numerical vector containing sex, coded 0 for males, 1 for females and -1 for unknown
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_terms	A boolean variable determining whether dominance terms for the variants should be included as covariates in the analysis

`covariates` A dataframe containing any other covariates that should be used; one column per covariate

### Value

A list with the interaction effect (on log-scale) and corresponding standard error, z statistic and p-value

### Examples

```
g1_vec <- rbinom(100000, 2, 0.9)
g2_vec <- rbinom(100000, 2, 0.1)
cc_vec <- rbinom(100000, 1, 0.1 * (1.05^g1_vec) *
  (1.05^g2_vec) * (1.3 ^ (g1_vec * g2_vec)))
res <- interaction_CC.calc(cc_vec, g1_vec, g2_vec)
```

---

kappa\_calc

*Genetic correlation effects*

---

### Description

This function estimates the correlation effect of a genetic variant on a pair of quantitative traits. The effect ( $\kappa$ ) is measured on Fisher transformed correlation values. The genotype is coded as 0 (non-carrier), 1 (single copy of effect allele) and 2 (two copies of effect allele). We use a likelihood ratio test with 1 degree of freedom: \*  $H_0: z_0 = z_1 = z_2$ , \*  $H_1: z_j = z_{\text{null}} + \kappa * j$ , where  $z_j$  is the Fisher-transformed correlation between the traits amongst subjects of genotype  $j$ .

If the traits follow a joint normal distribution, then (thoretically) the Fisher-transformed sample correlation ( $z$ ) is approximately normally distributed with mean 0 and standard error  $1/\sqrt{n-3}$ . Otherwise, we have to correct for possible bias in the estimators and scale the weights we assign to them appropriately

Note, that even though each trait follows a normal distribution individually, that does not necessarily imply that the pair of them follow a joint normal distribution.

### Usage

```
kappa_calc(qt1, qt2, g, weight_scale = 1, bias_scale = 0)
```

### Arguments

<code>qt1</code>	A numeric vector.
<code>qt2</code>	A numeric vector.
<code>g</code>	An integer vector.
<code>weight_scale</code>	Used to appropriately scale the weight assigned to the correlation estimators
<code>bias_scale</code>	Used to appropriately scale the bias of the correlation estimators

**Value**

A list with the values:

\* kappa, the estimated correlation effect \* pval, the p-value of the likelihood ratio test

**Examples**

```
Sigma0 <- matrix(c(1,0,0,1),nrow=2,ncol=2)
Sigma1 <- matrix(c(1,0.3,0.3,1),nrow=2,ncol=2)
Sigma2 <- matrix(c(1,0.6,0.6,1),nrow=2,ncol=2)
geno_vec <- c(rep(0,10000),rep(1,1000),rep(2,100))
Q0 <- MASS::mvrnorm(n = 10000, mu = c(0,0), Sigma = Sigma0)
Q1 <- MASS::mvrnorm(n = 1000, mu = c(0,0), Sigma = Sigma1)
Q2 <- MASS::mvrnorm(n = 100, mu = c(0,0), Sigma = Sigma2)
Q <- rbind(Q0,Q1)
Q <- rbind(Q,Q2)
qt1_val <- Q[,1]
qt2_val <- Q[,2]
res <- kappa_calc(qt1_val, qt2_val, geno_vec)
```

---

pairwise\_env\_int.calc *Pairwise environmental interaction effects*

---

**Description**

Given a set of variants and environmental traits, and a single quantitative trait, this function calculates the interaction effect of all possible variant-environmental pairs

**Usage**

```
pairwise_env_int.calc(
  qt,
  g,
  env,
  round_imputed = FALSE,
  dominance_term = FALSE,
  square_env = FALSE,
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0)),
  variant_names = paste(rep("variant", ncol(g)), as.character(1:ncol(g)), sep = "_"),
  env_names = paste(rep("env", ncol(env)), as.character(1:ncol(env)), sep = "_")
)
```

**Arguments**

qt	A numeric vector
g	A matrix, where each column represents a variant
env	A matrix, where each row represents an environmental variable

round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_term	A boolean variable determining whether a dominance term for the variant should be included as a covariates in the analysis
square_env	A boolean variable determining whether the square of the environmental trait should be included as a covariate in the analysis
covariates	A dataframe containing any other covariates that should be used; one column per covariate
variant_names	A list of the names of the variants
env_names	A list of the names of the environmental variables

**Value**

A dataframe with all possible variant-environmental pairs and their estimated interaction effect

**Examples**

```
g_vec <- matrix(0, nrow = 100000, ncol = 3)
freqs <- runif(ncol(g_vec), min = 0, max = 1)
env_vec <- matrix(0, nrow = 100000, ncol = 3)
for(i in 1:ncol(g_vec)){
  g_vec[, i] <- rbinom(100000, 2, freqs[i])
}
for( i in 1:ncol(env_vec)){
  env_vec[, i] <- round(runif(100000,min=0,max=6))
}

qt_vec <- rnorm(100000) + 0.1 * g_vec[, 1] + 0.2 *
  g_vec[, 2] -0.1 * env_vec[, 3] + 0.1 *
  env_vec[, 1] + 0.1 * g_vec[, 1] * env_vec[, 1]
res <- pairwise_env_int.calc(qt_vec, g_vec, env_vec)
```

---

pairwise\_env\_int\_CC.calc

*Pairwise environmental interaction effects for a case control variable*

---

**Description**

Given a set of variants and environmental traits, and a single case control variable, this function calculates the interaction effect of all possible variant-environmental pairs

**Usage**

```
pairwise_env_int_CC.calc(
  cc,
  g,
  env,
```

```

yob = rep(-1, length(cc)),
sex = rep(-1, length(cc)),
round_imputed = FALSE,
dominance_term = FALSE,
square_env = FALSE,
covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0)),
variant_names = paste(rep("variant", ncol(g)), as.character(1:ncol(g)), sep = "_"),
env_names = paste(rep("env", ncol(env)), as.character(1:ncol(env)), sep = "_")
)

```

### Arguments

cc	A numeric vector
g	A matrix, where each column represents a variant
env	A matrix, where each row represents an environmental variable
yob	A numerical vector containing year of birth. If some are unknown they should be marked as -1
sex	A numerical vector containing sex, coded 0 for males, 1 for females and -1 for unknown
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_term	A boolean variable determining whether a dominance term for the variant should be included as a covariates in the analysis
square_env	A boolean variable determining whether the square of the environmental trait should be included as a covariate in the analysis
covariates	A dataframe containing any other covariates that should be used; one column per covariate
variant_names	A list of the names of the variants
env_names	A list of the names of the environmental variables

### Value

A dataframe with all possible variant-environmental pairs and their estimated interaction effect

### Examples

```

N_run <- 25000
g_vec <- matrix(0, nrow = N_run, ncol = 3)
freqs <- runif(ncol(g_vec), min = 0, max = 1)
env_vec <- matrix(0, nrow = N_run, ncol = 3)
for(i in 1:ncol(g_vec)){
  g_vec[, i] <- rbinom(N_run, 2, freqs[i])
}
for( i in 1:ncol(env_vec)){
  env_vec[, i] <- round(runif(N_run,min=0,max=6))
}
cc_vec <- rbinom(N_run,1,0.1 * (1.05 ^ g_vec[, 1]) *

```

```

      (1.06 ^ env_vec[,1]) * (0.95 ^ g_vec[, 2]) *
      (1.1^(g_vec[, 1] * env_vec[, 1]))
res <- pairwise_env_int_CC.calc(cc_vec, g_vec, env_vec)

```

---

pairwise\_int.calc      *Pairwise interaction effects*

---

## Description

Given a set of variants and a quantitative trait, this function calculates the interaction effect of all possible variant-variant pairs

## Usage

```

pairwise_int.calc(
  qt,
  g,
  round_imputed = FALSE,
  dominance_terms = FALSE,
  variant_names = paste(rep("variant", ncol(g)), as.character(1:ncol(g)), sep = "_"),
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0))
)

```

## Arguments

qt	A numeric vector
g	A matrix, where each column represents a variant
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_terms	A boolean variable determining whether dominance terms for the variants should be included as covariates in the analysis
variant_names	A list of the names of the variants
covariates	A dataframe containing any other covariates that should be used; one column per covariate

## Value

A dataframe with all possible variant pairs and their estimated interaction effect

**Examples**

```

g_vec <- matrix(0, nrow = 100000, ncol = 5)
freqs <- runif(ncol(g_vec), min = 0, max = 1)
for(i in 1:ncol(g_vec)){
  g_vec[,i] <- rbinom(100000, 2, freqs[i])
}

qt_vec <- rnorm(100000) + 0.1 * g_vec[, 1] + 0.2 *
  g_vec[, 2] - 0.1 * g_vec[, 3] + 0.2 *
  g_vec[, 1] * g_vec[, 2]
res <- pairwise_int.calc(qt_vec, g_vec)

```

---

pairwise\_int\_CC.calc *Pairwise interaction effects for a case control variable*

---

**Description**

Given a set of variants and a case control variable, this function calculates the interaction effect of all possible variant-variant pairs

**Usage**

```

pairwise_int_CC.calc(
  cc,
  g,
  yob = rep(-1, length(cc)),
  sex = rep(-1, length(cc)),
  round_imputed = FALSE,
  dominance_terms = FALSE,
  covariates = as.data.frame(matrix(0, nrow = 0, ncol = 0)),
  variant_names = paste(rep("variant", ncol(g)), as.character(1:ncol(g)), sep = "_")
)

```

**Arguments**

cc	A numeric vector
g	A matrix, where each column represents a variant
yob	A numerical vector containing year of birth. If some are unknown they should be marked as -1
sex	A numerical vector containing sex, coded 0 for males, 1 for females and -1 for unknown
round_imputed	A boolean variable determining whether imputed genotype values should be rounded to the nearest integer in the analysis.
dominance_terms	A boolean variable determining whether dominance terms for the variants should be included as covariates in the analysis

covariates      A dataframe containing any other covariates that should be used; one column per covariate

variant\_names    A list of the names of the variants

### Value

A dataframe with all possible variant pairs and their estimated interaction effect

### Examples

```
N_run <- 25000
g_vec <- matrix(0, nrow = N_run, ncol = 5)
freqs <- runif(ncol(g_vec), min = 0, max = 1)
for(i in 1:ncol(g_vec)){
  g_vec[, i] <- rbinom(N_run, 2, freqs[i])
}
cc_vec <- rbinom(N_run, 1, 0.1 * (1.05 ^ g_vec[, 1]) *
  (1.06 ^ g_vec[, 2]) * (0.95 ^ g_vec[, 3]) *
  (1.5^(g_vec[, 1] * g_vec[, 2])))
res <- pairwise_int_CC.calc(cc_vec, g_vec)
```

---

PRS\_creator

*Creates polygenic risk scores*

---

### Description

This function creates genetic risk scores, with the option of including interactions or dominance effects. The score is automatically shifted to have mean 0.

### Usage

```
PRS_creator(
  g,
  betas,
  dominance_effects = rep(0, length(betas)),
  interaction_effects = matrix(0, nrow = 0, ncol = 0),
  log_scale = FALSE
)
```

### Arguments

g                      A matrix, where each column represents a variant and each line represents a subject

betas                  A numeric vector, representing the (additive) effects of the variants

dominance\_effects    A numeric vector, representing dominance effects of the variants

`interaction_effects` A matrix with three columns. First two columns are integers that correspond to the variants that are interacting. The third column is the effect size.

`log_scale` A Boolean variable. If true all analysis is done on log-transformed effect values and the resulting score is transformed back to an exponential scale in the end.

**Value**

A numeric vector with a polygenic risk score for each subject

**Examples**

```
g_vec <- matrix(0, nrow = 100000, ncol = 5)
freqs <- runif(ncol(g_vec), min = 0, max = 1)
for(i in 1:ncol(g_vec)){
  g_vec[,i] <- rbinom(100000, 2, freqs[i])
}
beta_vec <- runif(5, min = -0.5, max = 0.5)
dom_vec <- runif(5, min = -0.5, max = 0.5)
int_vec <- matrix(0, nrow = 2, ncol = 3)
int_vec[, 1] <- c(1, 3)
int_vec[, 2] <- c(2, 5)
int_vec[, 3] <- runif(2, min = -0.5, max = 0.5)
res <- PRS_creator(g_vec, beta_vec, dominance_effects = dom_vec, interaction_effects = int_vec)
```

---

`train_and_impute_PRS` *Trains and imputes a polygenic risk score (PRS)*

---

**Description**

This function trains a polygenic risk score model on a dataset, and then imputes the risk score into another dataset

**Usage**

```
train_and_impute_PRS(
  qt_training,
  g_training,
  g_impute,
  dominance_effects = rep(FALSE, ncol(g_training)),
  interaction_effects = matrix(0, nrow = 0, ncol = 0)
)
```

**Arguments**

`qt_training` A numeric vector. Represents the qt values of the data we train the model on.

`g_training` A matrix, where each column represents a variant and each line represents a subject in the training data

`g_impute` A matrix, where each column represents a variant and each line represents a subject.

`dominance_effects` A Boolean vector, each term determines whether a dominance term for the corresponding variant is used in the model.

`interaction_effects` An integer matrix with two columns. Each line represents a pair of interacting variants that should be included in the model.

### Value

Returns a list with the following objects \* `PRS_imputed`, the imputed PRS values \* `PRS_training`, the PRS values for the training data \* `Residuals_training`, the residuals from the model in the training data

### Examples

```
g_train_vec <- matrix(0, nrow = 100000, ncol = 5)
freqs <- runif(ncol(g_train_vec), min = 0, max = 1)
for(i in 1:ncol(g_train_vec)){
  g_train_vec[,i] <- rbinom(100000, 2, freqs[i])
}
g_impute_vec <- matrix(0, nrow = 50000, ncol = 5)
for(i in 1:ncol(g_impute_vec)){
  g_impute_vec[,i] <- rbinom(50000, 2, freqs[i])
}
dom_vec <- c(TRUE, FALSE, FALSE, TRUE, FALSE)

int_vec <- matrix(c(1, 2, 4, 5), nrow = 2, ncol = 2)

qt_vec <- rnorm(100000) + 0.2 * g_train_vec[, 1] + 0.3 * g_train_vec[, 1] * g_train_vec[, 4]

res <- train_and_impute_PRS(qt_vec, g_train_vec, g_impute_vec,
  dominance_effects = dom_vec, interaction_effects = int_vec)
```

---

var.adj

*Mean and variance effect adjustments.*

---

### Description

Given is a set of (continuous) variables and a qt trait. First, this function adjusts the trait for the mean effects of the variables with a linear model. Next, the variance effect of the variables are estimated and the trait is adjusted further by scaling it in accordance with the results.

### Usage

```
var.adj(qt, x, iter_num = 50, eps_param = 1e-10)
```

**Arguments**

qt	A numeric vector.
x	A numeric matrix, each column represents a covariate.
iter_num	An integer. Represents the number of iterations performed in the Gauss-Newton algorithm
eps_param	A number. The Gauss-Newton algorithm terminates if the increment change of all variance estimates is smaller than this number.

**Value**

A vector, representing the adjusted trait.

**Examples**

```
n_val <- 50000
x <- matrix(0,nrow = n_val, ncol = 4)
for(i in 1:4) {
  x[, i] <- rnorm(n_val)
}
var_vec <- exp(0.2 * x[, 1] - 0.3 * x[, 4])
qt_vec <- rnorm(n_val, 0, sqrt(var_vec))
res <- var.adj(qt_vec, x)
```

---

 Var.assoc

*Uncertainty association*


---

**Description**

This function finds the association between the predicted uncertainty of some estimates of a trait to the "actual uncertainty" of the estimates. Suppose we have estimates of some trait (this might be a polygenic risk score). Moreover, suppose we have assigned a variance value to each estimate (this might be a variance risk score) to reflect how certain we believe we are about each estimate. Given the true trait values, this function evaluates how well the assigned variance values reflect reality.

We use a likelihood ratio test with 1 degree of freedom \* H0:  $y \sim N(\mu + b * m\_score, \sigma\_sq)$ , \* H1:  $y \sim N(\mu + b * m\_score, \sigma\_sq * (v\_score)^a)$ , where  $y$  is the trait  $m\_score$  is the estimate of the trait and  $v\_score$  is the variance assigned to the estimate. Thus H0 has three degrees of freedom  $(\mu, b, \sigma\_sq)$ , whereas H1 has four  $(\mu, b, \sigma\_sq, a)$

**Usage**

```
Var.assoc(qt, m_score, v_score, iter = 50)
```

**Arguments**

qt	A numeric vector.
m_score	A numeric vector
v_score	A numeric vector with positive values
iter	A number of iterations for the Gauss-Newton algorithm

**Value**

A list with the values:

\* a, the association between v\_score and the actual variance. \* pval, the p-value of the likelihood ratio test

**Examples**

```
n_val <- 50000L
trait_vec <- rnorm(n_val,0,1)
var_vec <- exp(rnorm(n_val,0,0.1))
est_vec <- trait_vec+rnorm(n_val,0,var_vec)
res <- Var.assoc(trait_vec,est_vec,var_vec, iter = 20)
```

---

var.summary

*Variance summary statistics*


---

**Description**

Estimates the variance effect of several continuous variables jointly

**Usage**

```
var.summary(qt, x, iter_num = 50, eps_param = 1e-10)
```

**Arguments**

qt	A numeric vector.
x	A data frame, each column represents a covariate that should be numeric.
iter_num	An integer. Represents the number of iterations performed in the Gauss-Newton algorithm
eps_param	A number. The Gauss-Newton algorithm terminates if the increment change of all variance estimates is smaller than this number.

**Value**

A list with the following objects: \* summary, a dataframe with a variance effect estimate for each variable and summary statistics \* chi2, the chi2 statistic obtained by considering all parameteres jointly \* df, degrees of freedom for the chi2 statistic \* pval, p-value of the model \* adjusted\_values, a vector with qt values that have been adjusted for both mean and variance effects

**Examples**

```
n_val <- 50000
x <- as.data.frame(matrix(0,nrow = n_val, ncol = 4))
colnames(x) <- c('A','B','C','D')
for(i in 1:4) {
  x[, i] <- rnorm(n_val)
}
var_vec <- exp(0.2 * x[, 1] - 0.3 * x[, 4])
qt_vec <- rnorm(n_val, 0, sqrt(var_vec))
res <- var.summary(qt_vec, x)
```

---

VarGS.plot

*Actual variance vs predicted variance plot*


---

**Description**

This tool creates a line plot that compares the predicted variance of data to its actual variance.

**Usage**

```
VarGS.plot(
  qt,
  v_score,
  bins = 10,
  xlab = "Predicted variance",
  ylab = "Variance",
  title = ""
)
```

**Arguments**

qt	A numeric vector.
v_score	A numeric vector.
bins	An integer.
xlab	A string.
ylab	A string.
title	A string.

**Value**

A plot comparing predicted variance to actual variance.

**Examples**

```
n_val <- 100000L
v_vec <- exp(rnorm(n_val, 0, 0.1))
qt_vec <- stats::rnorm(n_val, 0, sqrt(v_vec))
VarGS.plot(qt_vec, v_vec)
```

---

`Viol.by.gen`*Violin plot by genotype*

---

**Description**

This tool creates violin plots corresponding to each genotype.

**Usage**

```
Viol.by.gen(qt, g, trait_name = "qt trait", title = "")
```

**Arguments**

<code>qt</code>	A numeric vector.
<code>g</code>	An integer vector.
<code>trait_name</code>	A string.
<code>title</code>	A string.

**Value**

A violin plot

**Examples**

```
n_val <- 50000L
geno_vec <- sample(c(0, 1, 2), size = n_val, replace = TRUE)
qt_vec <- rnorm(n_val) * (1.3^geno_vec) + 1 * geno_vec
Viol.by.gen(qt_vec, geno_vec)
```

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